

**Department of Communications**

**Engineering**

**Communication Systems**

**Third Year Class**

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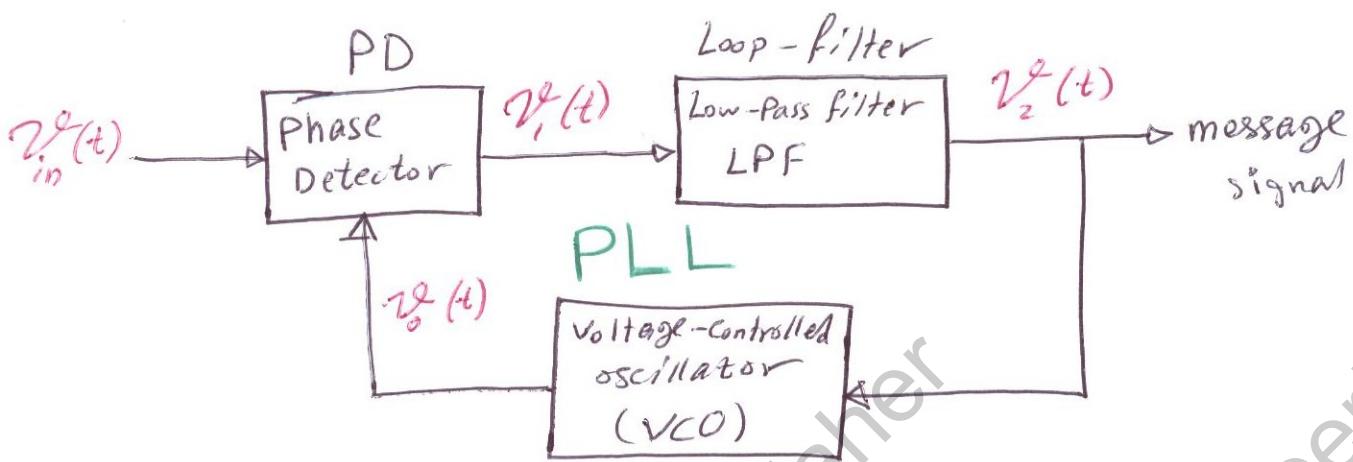
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**Lecture 10**

**Phase Locked Loop**

# Phase-Locked Loop : PLL

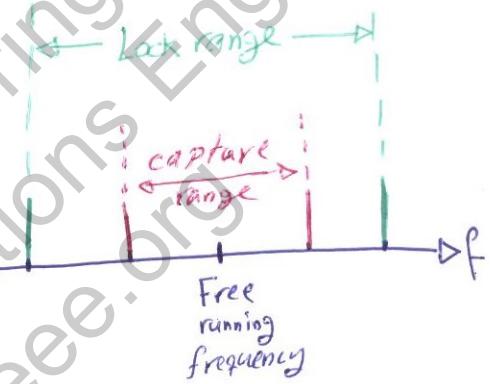
- \* All the previous methods are non-coherent Demodulation method for FM signals.
- \* PLL is a coherent method indirect FM Demodulation.
- \* PLL consists of :-
  - ① Phase Detector (PD).
  - ② Loop Filter (Low Pass Filter).
  - ③ Voltage Controlled oscillator (VCO).
- \* There are two types of PLL
  - ① Analog
  - ② Digital



The PLL has three states

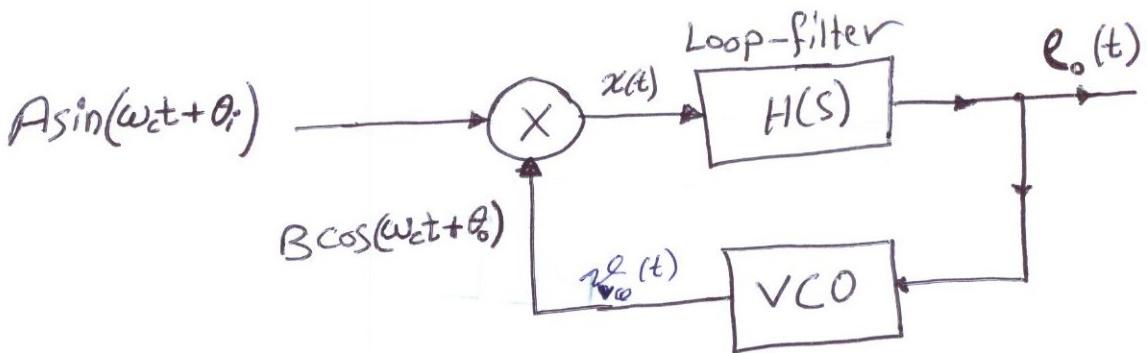
① Free running state,

will be defined soon  
 ② Capture state, and  
 ③ Lock range (Hold-in range) state



\* Free running  $\Rightarrow$  is the frequency when there is no input to the VCO.

$$\text{or } V_2^o(t) = 0$$



\* Suppose the VCO frequency oscillation is:

$$\omega(t) = \omega_c + c e_o(t) \quad (1)$$

$c$  is the VCO constant  
 $\omega_c$  is the free running VCO frequency.

\* Let the VCO output be

$$\omega_{vco}(t) = B \cos(\omega_c t + \theta_o) \quad (2)$$

\* Let the input to the PLL be

$$x_{in}(t) = A \cos(\omega_i t + \theta_i) \quad (3)$$

$$\therefore x(t) = AB \sin(\omega_i t + \theta_i) \cos(\omega_c t + \theta_o)$$

$$x(t) = \frac{AB}{2} [\sin(\theta_i - \theta_o) + \underbrace{\sin(2\omega_c t + \theta_i + \theta_o)}_{\text{suppressed by the narrowband LPF Loop Filter}}] \quad (4)$$

$$\therefore e_o(t) = \frac{AB}{2} \underbrace{\sin(\theta_i - \theta_o)}_{\theta_e} \quad (5)$$

\* Suppose that the loop is locked :

$\therefore$  input frequency to the PD & output frequency from the PLL are identical.

$\therefore \theta_i, \theta_o, \& \theta_e$  are constants

\* Suppose the input frequency increased suddenly

$$v_{in}^e(t) = A \cos[(\omega_c + k)t + \theta_i] \quad (6)$$

or

$$v_{in}^e(t) = A \cos(\omega_c t + \hat{\theta}_i) \quad (7)$$

$$\text{where } \hat{\theta}_i = kt + \theta_i \quad (8)$$

Thus, the increase in the incoming frequency causes  $\theta_i$  to increase

$$\theta_i \rightarrow \theta_i + kt \rightarrow \theta_e \text{ increased}$$

Hence  $\theta_o(t)$  increases, leading to increase in the output of the VCO frequency

\* Suppose the incoming frequency decreased suddenly :-

$$\therefore \theta_i \rightarrow \theta_i - kt \rightarrow \theta_e \text{ decreased}$$

$\therefore$  the output frequency of the VCO decreased

Thus, the PLL tracks the input sinusoid. The two signals are said to be mutually phase coherent or in phase lock.

\* A PLL can track the incoming frequency over a finite range

\* the PLL tracks the frequency change over a range of frequencies,

\* the tracking range is called Hold-in or Lock range.

\* If input / output frequencies are not close enough the loop may not lock.

The range of frequencies over which the input will cause the loop to lock is called pull-in or capture range.