University Of Diyala College Of Engineering Computer Engineering Department



1

# Digital System Design II

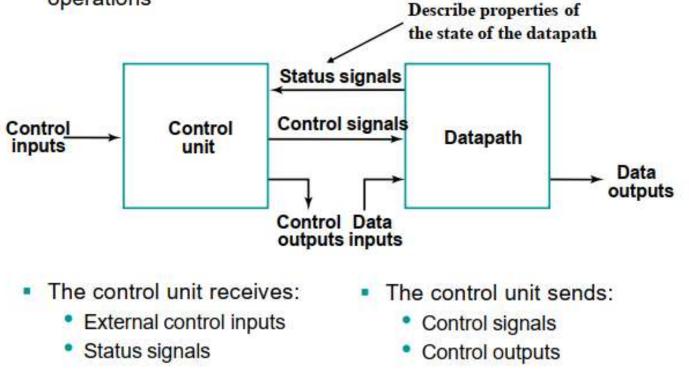
Dr. Yasir Amer Al-Zubaidi Third stage 2021

### Design of Digital Sequential Circuits Using New Methods *Microprogramming Overview*

- Data path and Control
- Microoperations
- Sequencing and control

#### **Datapath and Control**

- Datapath performs data transfer and processing operations
- Control Unit Determines the enabling and sequencing of the operations



#### Overview

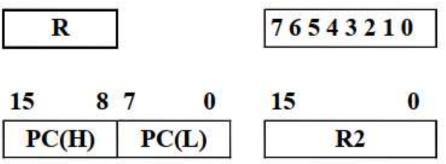
- Datapath and control
- Microoperations
  - Register transfer operations
  - Microoperations arithmetic, logic, and shift
  - Register cell design
  - Serial transfers and microoperations
- Sequencing and control

# **Register Transfer Operations**

- Register Transfer Operations the movement and processing of data stored in registers
- Three basic components:
  - A set of registers (operands)
  - Transfer operations
  - Control of operations
- Elementary operations -- called microoperations
  - Ioad, count, shift, add, bitwise "OR", etc.

#### **Register Notation**

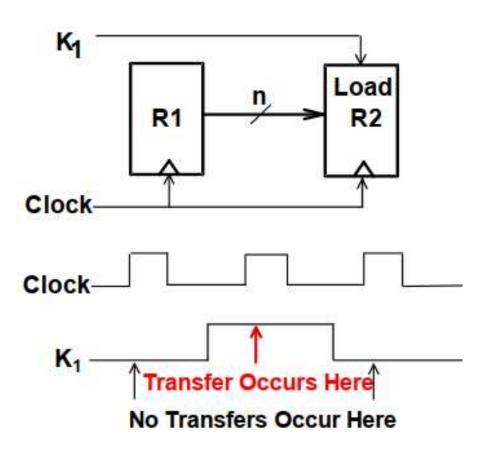
- Letters and numbers register (e.g. R2, PC, IR)
- Parentheses () range of register bits (e.g. R1(1), PC(7:0), AR(L))



- Arrow ( $\leftarrow$ ) data transfer (ex. R1  $\leftarrow$  R2, PC(L)  $\leftarrow$  R0)
- Brackets [] Specifies a memory address (ex. R0 ← M[AR], R3 ← M[PC] )
- Comma separates parallel operations

#### **Conditional Transfer**

If (K<sub>1</sub> =1) then (R2 ← R1)
 ⇔ K<sub>1</sub>: (R2 ← R1)
 where K<sub>1</sub> is a control expression specifying a conditional execution of the microoperation.



## **Microoperations**

- Logical groupings:
  - Transfer move data from one set of registers to another
  - Arithmetic perform arithmetic on data in registers
  - Logic manipulate data or use bitwise logical operations
  - Shift shift data in registers

Arithmetic operations

- + Addition
- Subtraction
- \* Multiplication
- / Division

Logical operations ∨ Logical OR ∧ Logical AND ⊕ Logical Exclusive OR Not

# **Example Microoperations**

- R1← R1 + R2
  - Add the content of R1 to the content of R2 and place the result in R1.
- PC ← R1 \* R6
- R1  $\leftarrow$  R1  $\oplus$  R2
- (K1 + K2): R1 ← R1 ∨ R3
  - On condition K1 <u>OR</u> K2, the content of R1 is <u>Logic bitwise</u> <u>Ored</u> with the content of R3 and the result placed in R1.
  - NOTE: "+" (as in K<sub>1</sub> + K<sub>2</sub>) means "OR." In R1 ← R1 + R2, + means "plus."

# **Arithmetic Microoperations**

Symbolic Designation	Description	
$R0 \leftarrow R1 + R2$	Addition	
$R0 \leftarrow \overline{R1}$	<b>Ones Complement</b>	
$R0 \leftarrow \overline{R1} + 1$	<b>Two's Complement</b>	
$R0 \leftarrow R2 + \overline{R1} + 1$	R2 minus R1 (2's Comp)	
$R1 \leftarrow R1 + 1$	Increment (count up)	
$R1 \leftarrow R1 - 1$	Decrement (count down)	

- Any register may be specified for source 1, source 2, or destination.
- These simple microoperations operate on the whole word

# **Logical Microoperations**

Symbolic Designation	Description	
$R0 \leftarrow \overline{R1}$	Bitwise NOT	
$R0 \leftarrow R1 \lor R2$	Bitwise OR (sets bits)	
$R0 \leftarrow R1 \land R2$	Bitwise AND (clears bits)	
$R0 \leftarrow R1 \oplus R2$ Bitwise EXOR (complements bit		

#### **Shift Microoperations**

Let R2 = 11001001

Symbolic Designation	Description	R1 content	
R1 ← sl R2	Shift Left	10010010	
R1 ← sr R2	Shift Right	01100100	

- Note: These shifts "zero fill". Sometimes a separate flip-flop is used to provide the data shifted in, or to "catch" the data shifted out.
- Other shifts are possible (rotates, arithmetic)

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1

# Digital System Design II

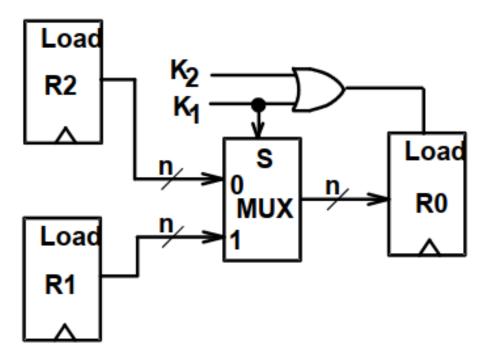
Dr. Yasir Al-Zubaidi

**Third stage** 

2019

# Multiplexer-Based Single Register Transfers

- MUX connected to register outputs produce flexible transfer structures
- Transfers: K1:  $\underline{R0} \leftarrow R1$ K2 K1: R0  $\leftarrow R2$



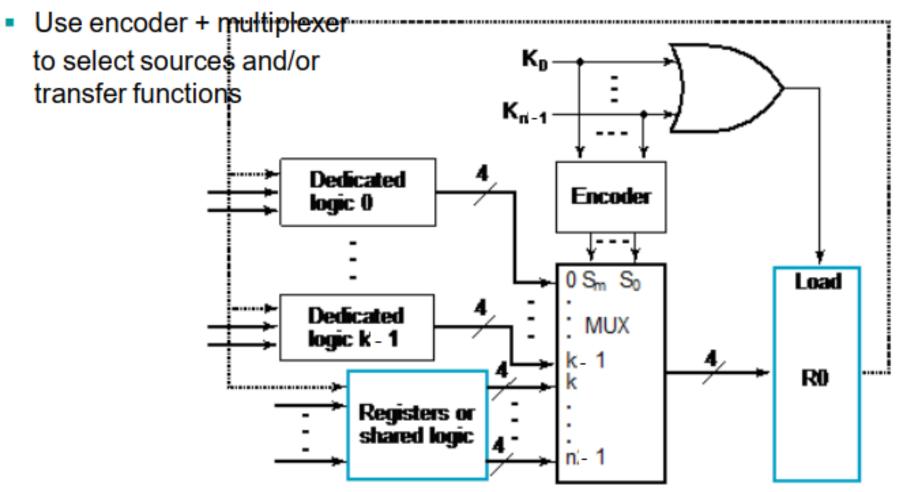


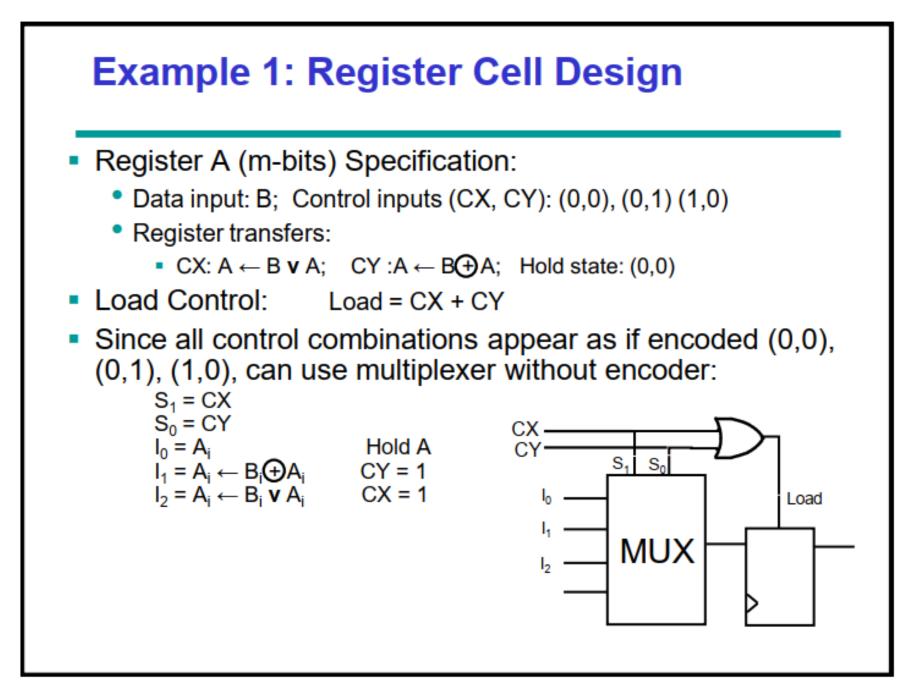
Assume: a register consists of identical cells

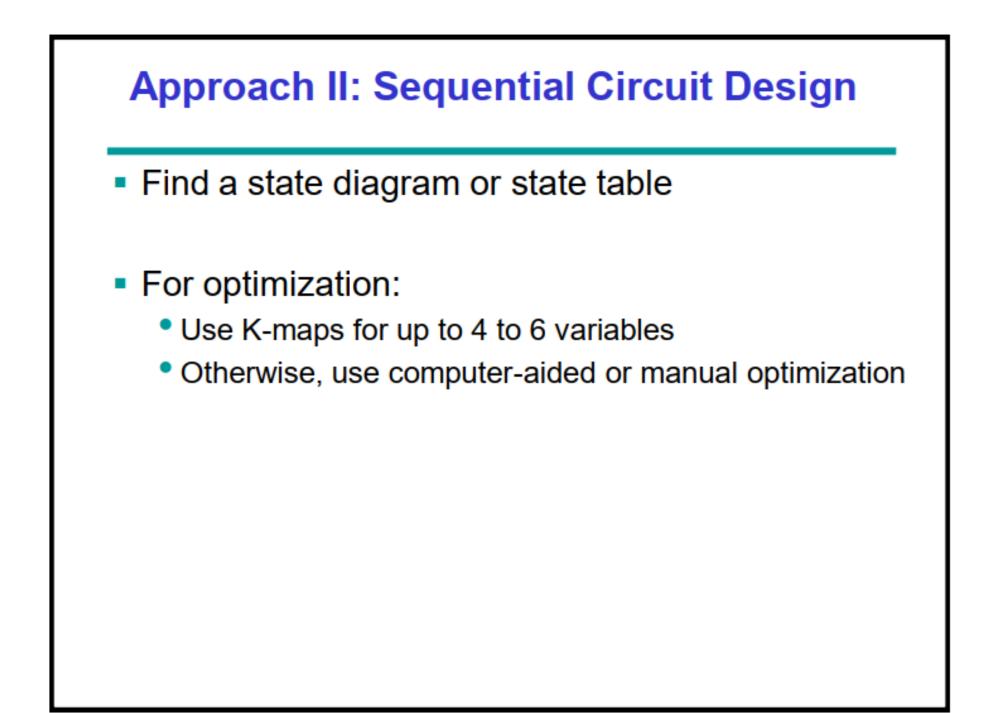
- Register design can be approached as follows:
  - Design a representative cell for the register
  - Make copies of the cell and connect together to form the register
  - Applying appropriate "boundary conditions" to cells that need to be different and contract if appropriate
- <u>Register cell design</u> is the first step of the above process

# **Approach I: Multiplexer-based**

- An n-input multiplexer with a variety of sources and functions
- Load enable by OR of control signals K<sub>0</sub>, K<sub>1</sub>, ... K<sub>n-1</sub> (for 00...0, no load)







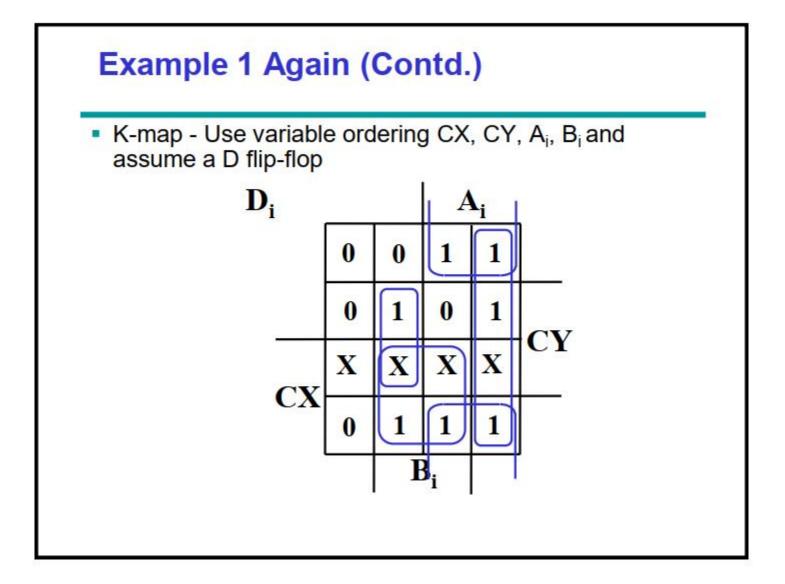
# Example 1 Again

#### State Table for D<sub>i</sub>:

	Hold	Ai <b>v</b> Bi		Ai⊕Bi	
	CX = 0	CX = 1	CX = 1	CX = 0	CX = 0
A <sub>i</sub>	CY = 0	CY = 0	CY = 0	CY = 1	CY = 1
		B <sub>i</sub> = 0	B <sub>i</sub> = 1	B <sub>i</sub> = 0	B <sub>i</sub> = 1
0	0	0	1	0	1
1	1	1	1	1	0

- Four variables (CX, CY, A, B) should give a total of 16 state table entries
- By using:
  - Combinations of variable names and values
  - Don't care conditions (for CX = CY = 1)

only 12 entries are required to represent the 16 entries



# Example 1 Again (Contd.)

 The resulting SOP equation: D<sub>i</sub> = CX B<sub>i</sub> + CY Ā<sub>i</sub> B<sub>i</sub> + A<sub>i</sub> B
i + CY A<sub>i</sub>

 = CX B<sub>i</sub> + Ā<sub>i</sub> (CY B<sub>i</sub>) + A<sub>i</sub>(CY B<sub>i</sub>)

 = CX B<sub>i</sub> + A<sub>i</sub> ⊕ (CY B<sub>i</sub>)

 The gate input cost per cell = 13

The gate input cost per cell for the previous version is:

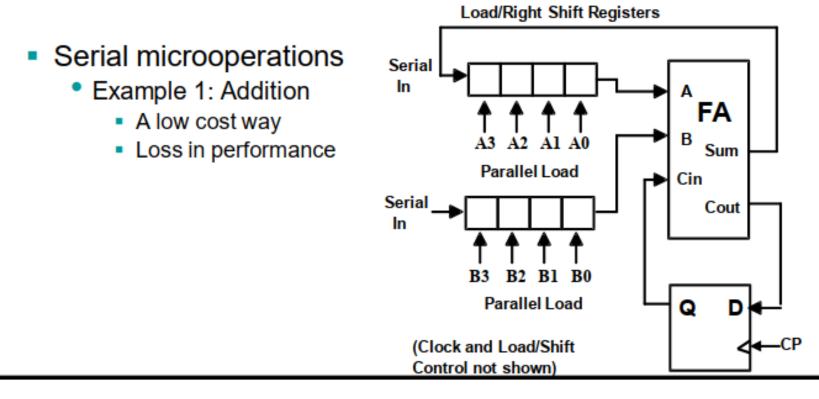
Per cell: 19 Shared decoder logic: 8

- Cost gain by sequential design > 6 per cell
- Also, no Enable on the flip-flop makes it cost less

#### **Serial Transfers and Microoperations**

#### Serial Transfers

- Used for "narrow" transfer paths
- Example 1: Telephone or cable line
  - <u>Parallel-to-Serial</u> conversion at source
  - Serial-to-Parallel conversion at destination



#### **Overview**

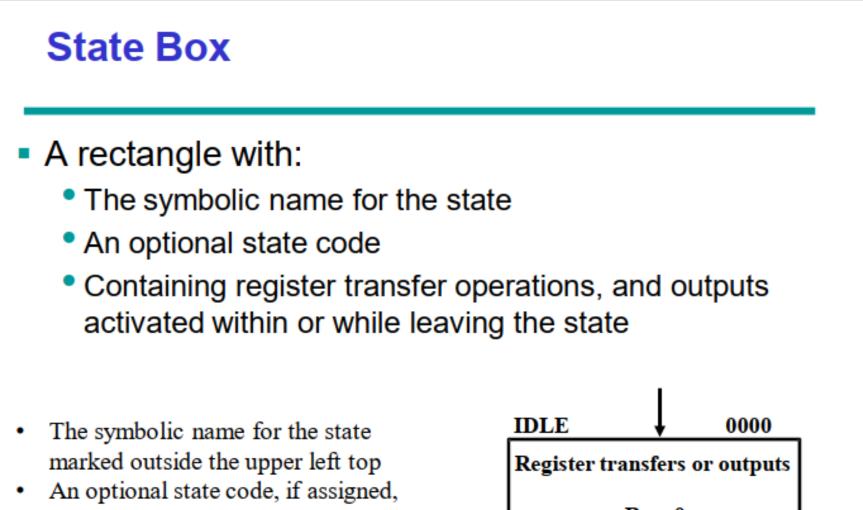
- Datapath and control
- Microoperations
- Sequencing and control
  - Algorithmic State Machines (ASM)
    - ASM chart
    - Timing considerations
    - ASM chart examples: Binary multiplier
  - Hardwired Control
    - Control design methods
    - Sequence register and decoder
    - One flip-flop per state
  - Microprogrammed control

#### **Control Unit Types**

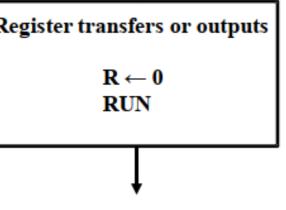
- Two distinct classes:
  - Programmable
  - Non-programmable.
- A programmable control unit:
  - An external memory array for storing instructions and control information
  - A program counter (PC) register points to the next instruction to be executed
  - Decision logic for determining the sequence of operations and logic to interpret the instructions
- A non-programmable control unit: does not fetch instructions from a memory and is not responsible for sequencing instructions

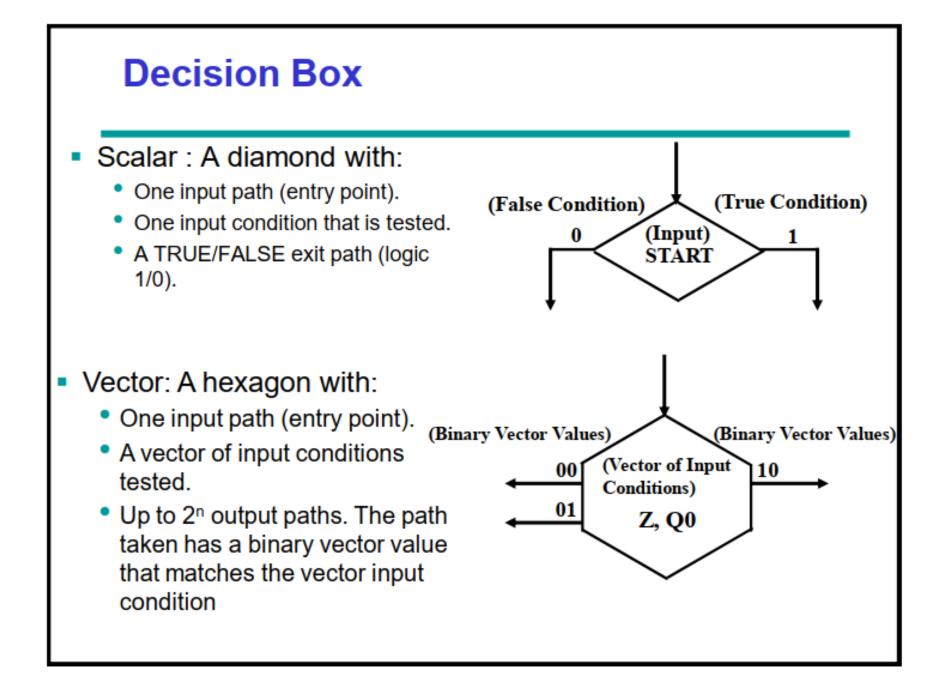
#### **Algorithmic State Machines**

- The function of a sequential circuit can be represented by a state table or a state diagram.
- An Algorithmic State Machine (ASM) is a flowchartlike way to specify state diagrams for sequential logic and, optionally, <u>actions performed in a datapath</u>.
  - A flowchart is a way of showing <u>actions</u> and <u>control flow</u> in an algorithm.
  - An ASM explicitly specifies a <u>sequence of actions</u> and their <u>timing</u> relationships
  - An ASM chart directly leads to a hardware realization
- Primitives:
  - 1. State Box (a rectangle)
  - 2. Decision Box
    - I. Scalar (a diamond)
    - II. Vector (a hexagon)
  - 3. Conditional Output Box (an oval)



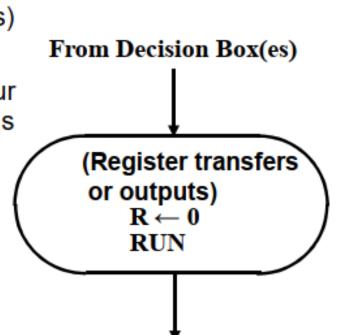
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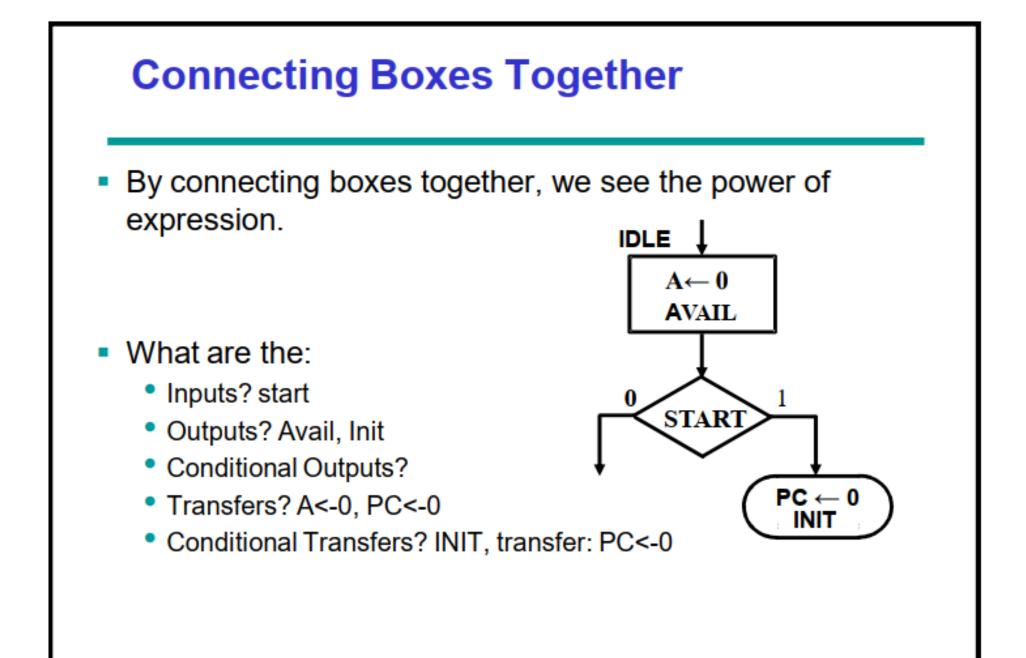




# **Conditional Output Box**

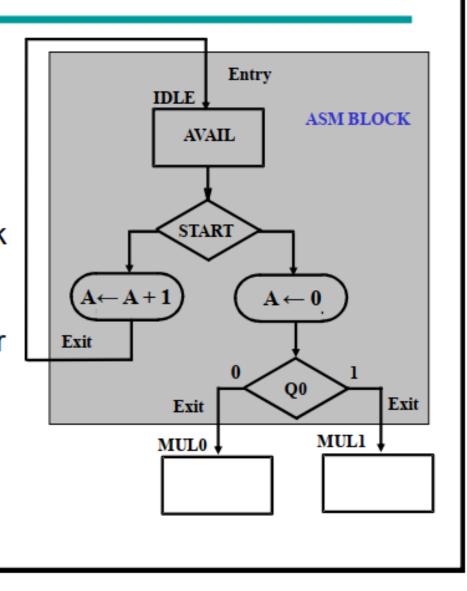
- An oval with:
  - One input path from a decision box(es)
  - One output path
  - Register transfers or outputs that occur only if the conditional path to the box is taken.
- Transfers and outputs
  - in a state box are <u>Moore type</u> dependent only on state
  - in a conditional output box are <u>Mealy</u> <u>type</u> - dependent on both state and inputs

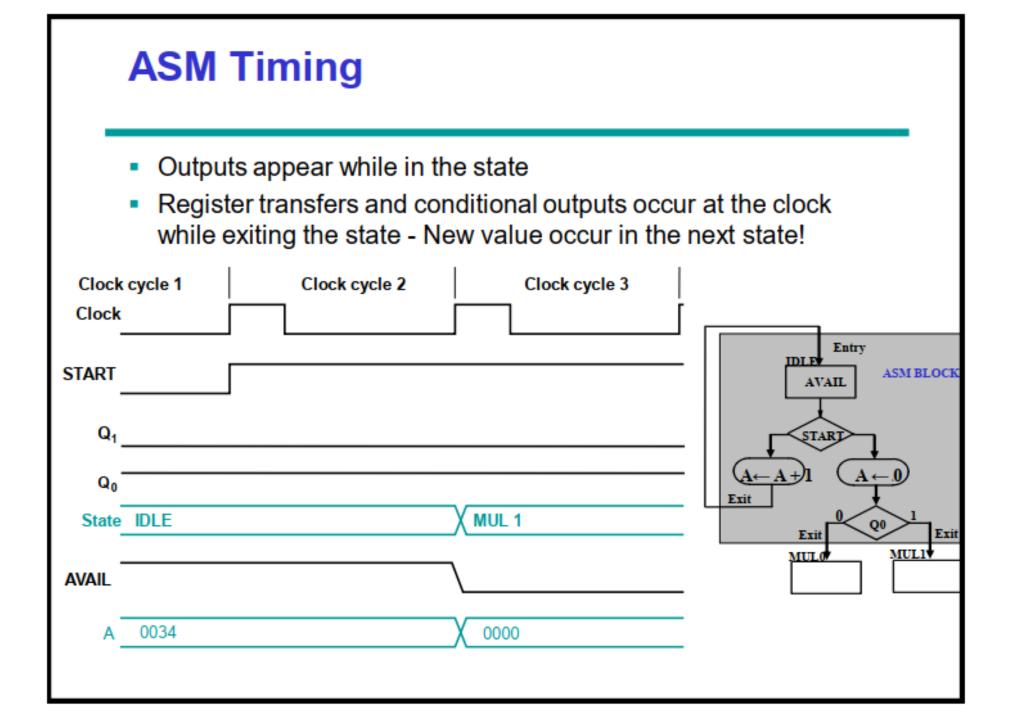


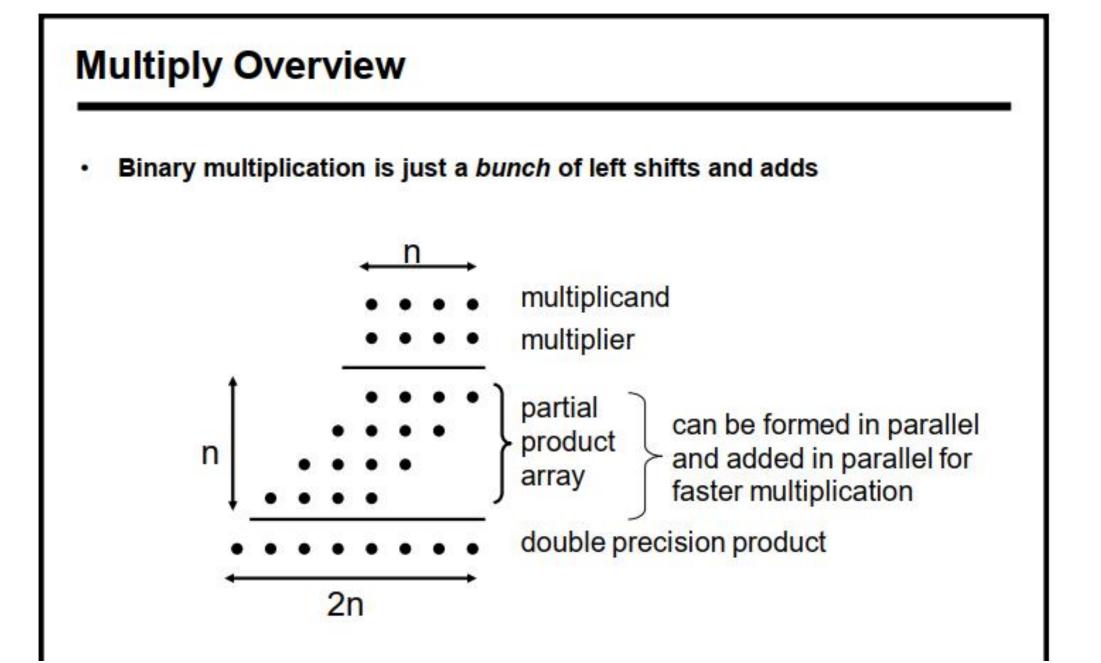


#### **ASM Blocks**

 One state box along with all decision and conditional output boxes connected to it, called an ASM Block. i.e., the ASM Block includes all items on the path from the current state to the same or other states.

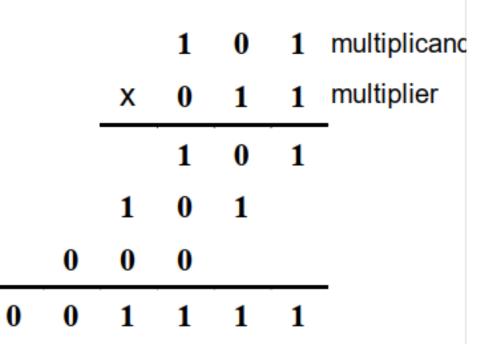


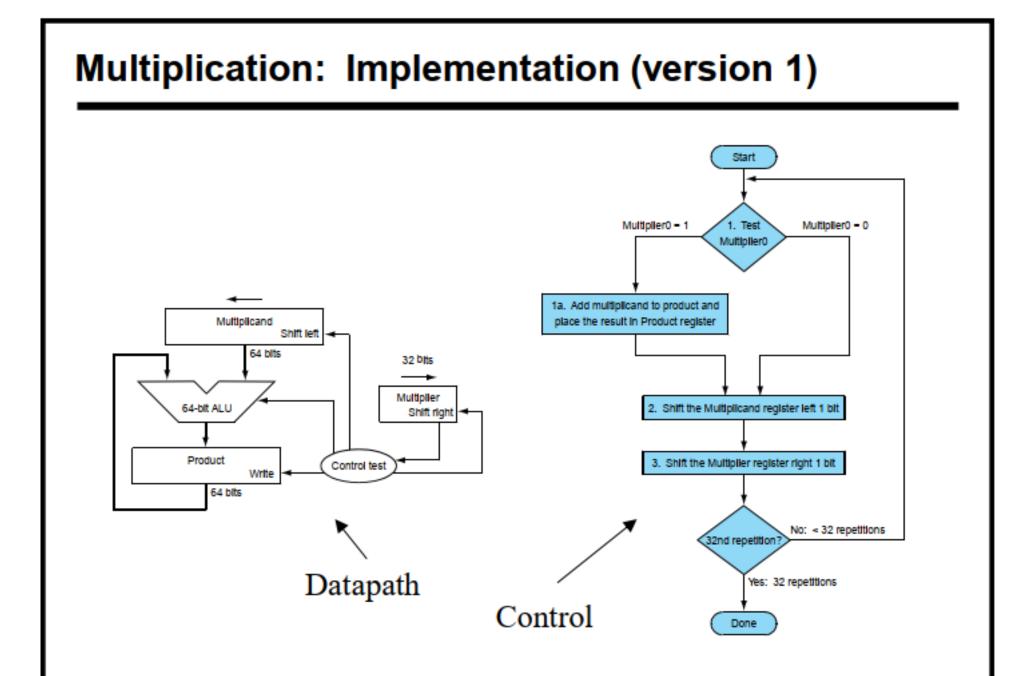


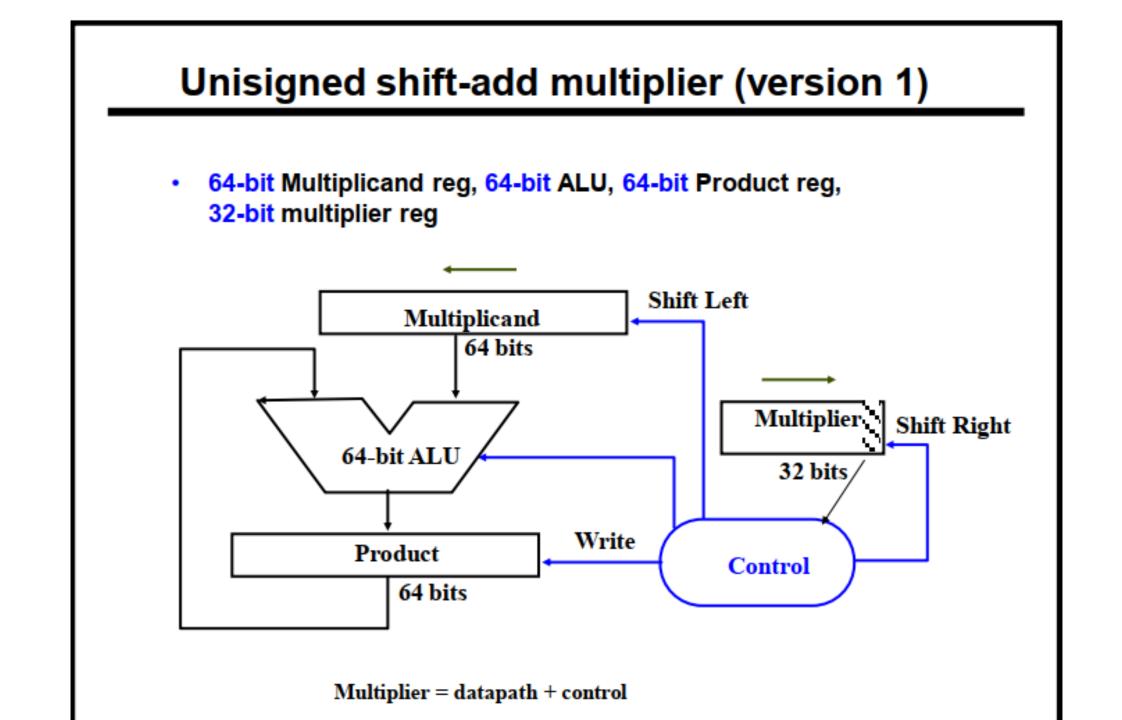


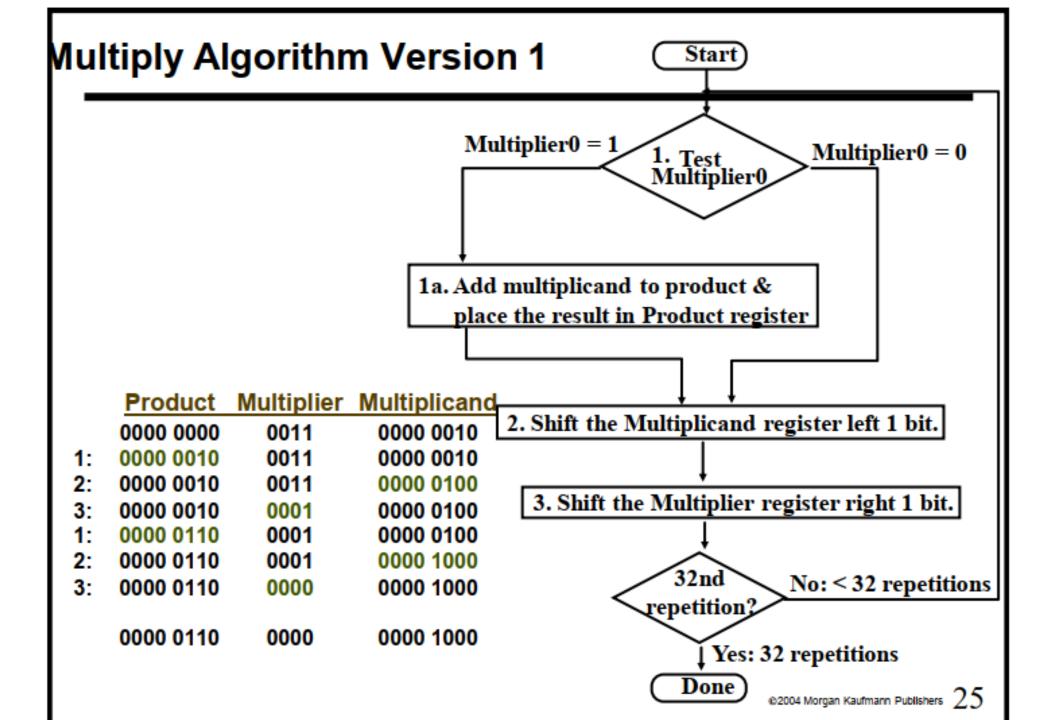
# **Multiplier Example**

- Example: (101 x 011) Base 2
- Partial products are: 101 x 0, 101 x 1, and 101 x 1







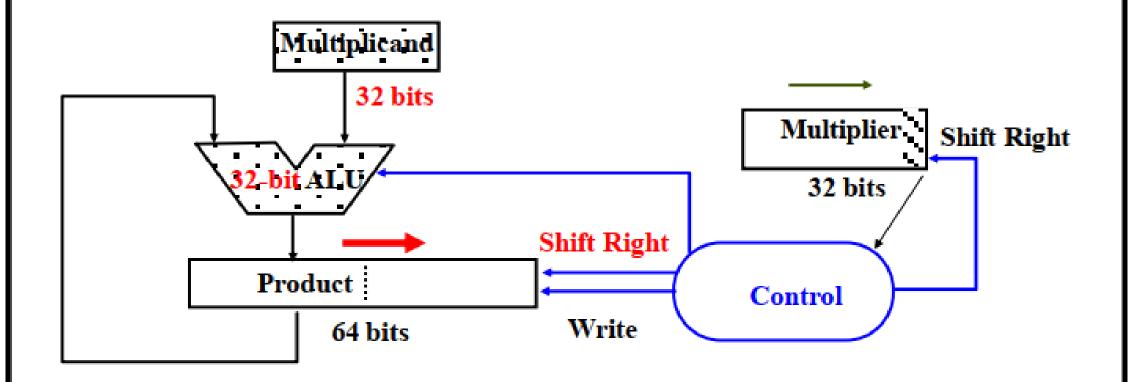


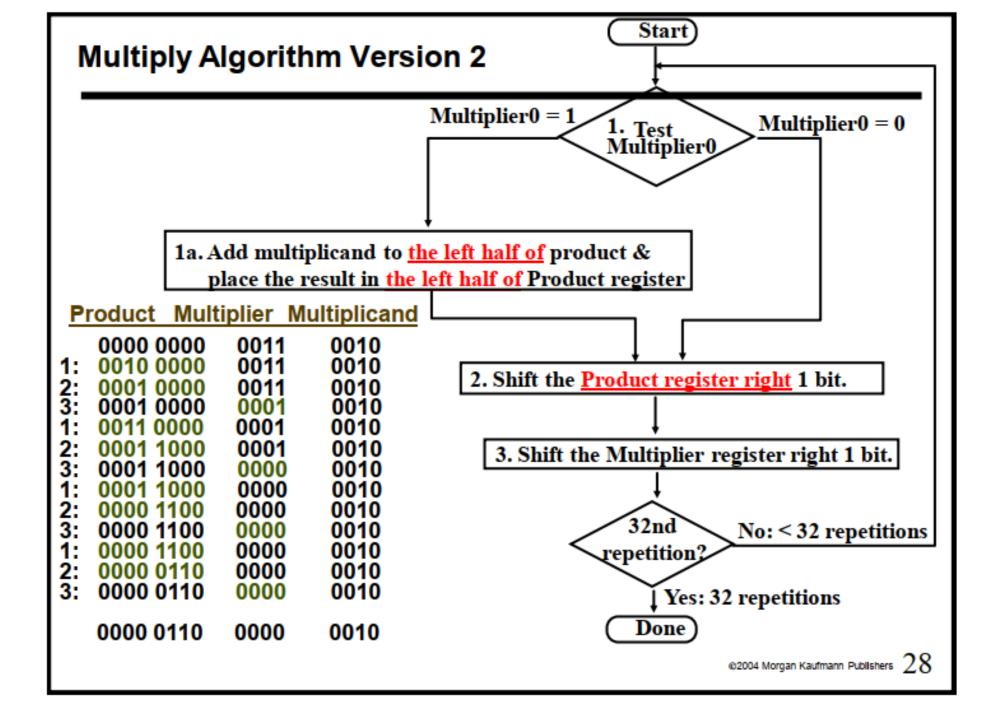
#### **Observations on Multiply Version 1**

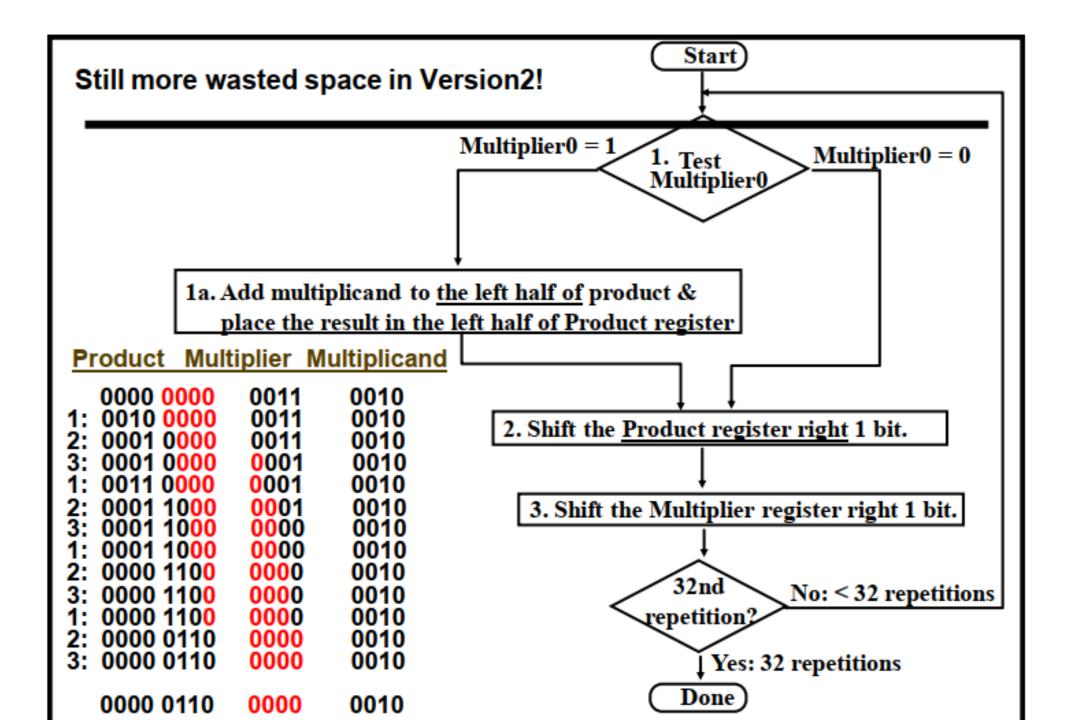
- 1 clock per cycle => ≈ 100 clocks per multiply because of 32 repetitions, 3 steps in one repetition
  - Ratio of add/sub to multiply is from 5:1 to 100:1
  - Slow
- 0's inserted in the rightmost bit of multiplicand as shifting left
  - => least significant bits of product never changed once formed
- 1/2 bits in multiplicand always 0
  - MSB are 0s at the beginning
  - 0 is inserted in LSB as multiplicand shifting left
  - => 64-bit multiplicand register is wasted
  - => 64-bit adder is wasted
- Instead of shifting multiplicand to left, let's <u>shift</u>
   product to right
   (2004 Morgan Kaufmann Publishers

## MULTIPLY HARDWARE Version 2

 <u>32</u>-bit Multiplicand reg, <u>32</u>-bit ALU, 64-bit Product reg, 32-bit Multiplier reg





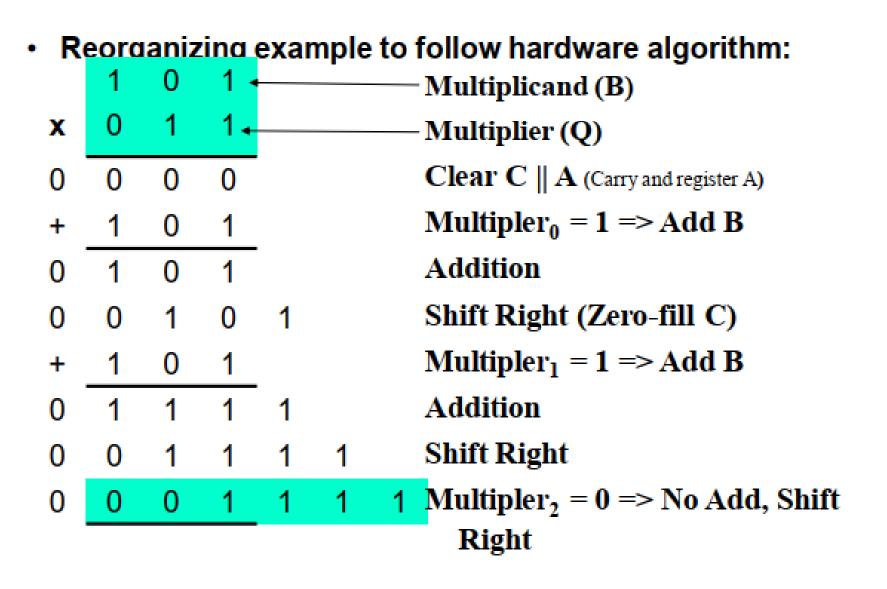


### **Observations on Multiply Version 2**

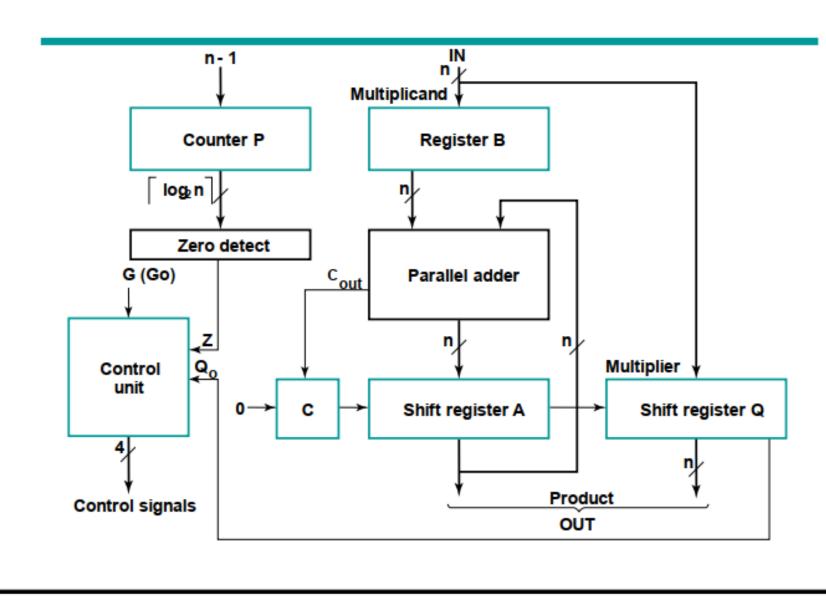
 Product register wastes space that exactly matches size of multiplier

=> combine Multiplier register and Product register

## Example (1 0 1) × (0 1 1) Again



### Multiplier Example: Block Diagram





- 1. The multiplicand is loaded into register B.
- 2. The multiplier is loaded into register Q.
- 3. When G becomes 1, register C|| A is initialized to 0.
- Down Counter P is initialized to n 1 (n = number of bits in multiplier)
- 5. The partial products are formed in register C||A||Q.
- 6. Each multiplier (Q) bit, beginning with the LSB, is processed (if bit is 1, B is added to partial product of A; if bit is 0, do nothing)
- 7. C||A||Q is shifted right using the shift register
  - Partial product bits fill vacant locations in Q as multiplier is shifted out
  - If overflow during addition, the outgoing carry is recovered from C during the right shift
- 8. Steps 6 and 7 are repeated until P = 0 as detected by Zero detect.

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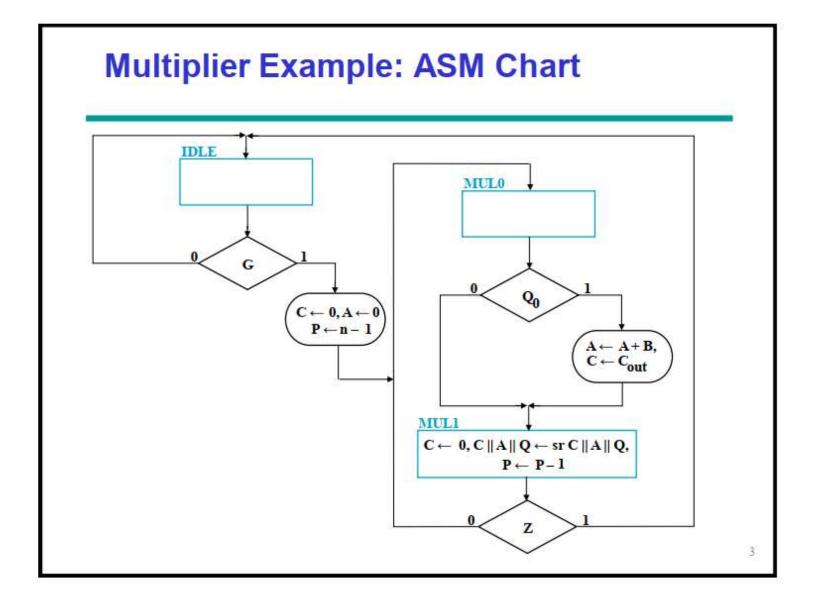
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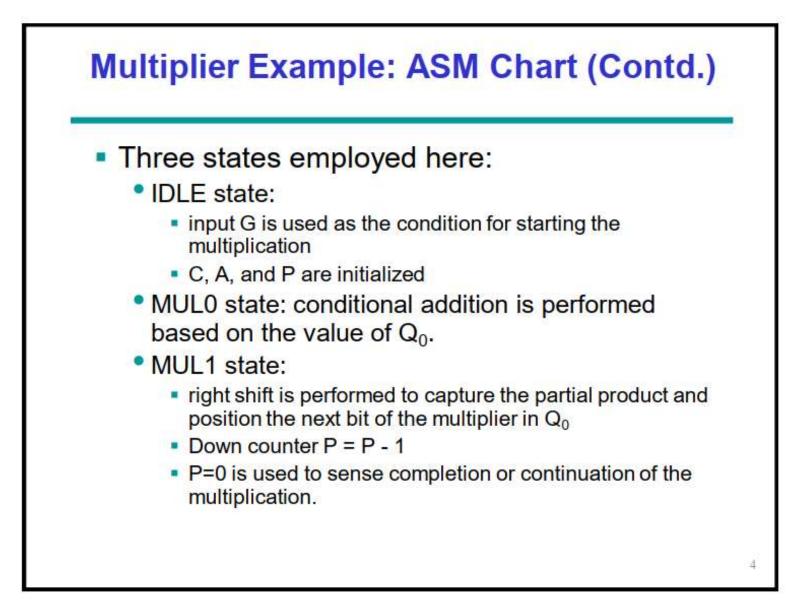
# Digital System Design II ASM Based Datapath and Control Design

Dr. Yasir Al-Zubaidi Third stage 2021

#### Overview

- Datapath and control
- Microoperations
- Sequencing and control
  - Algorithmic State Machines (ASM)
    - ASM chart
    - Timing considerations
    - ASM chart examples: Binary multiplier
  - Hardwired Control
    - Control design methods
    - Sequence register and decoder
    - One flip-flop per state
  - Microprogrammed control





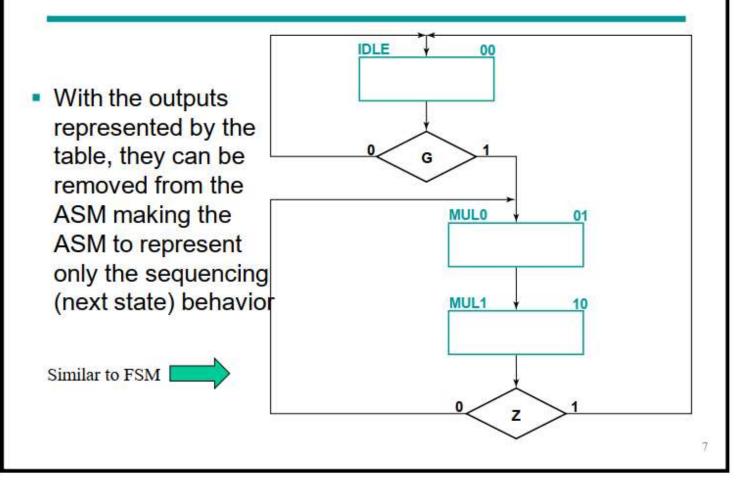
# Multiplier Example: Control Signal Table

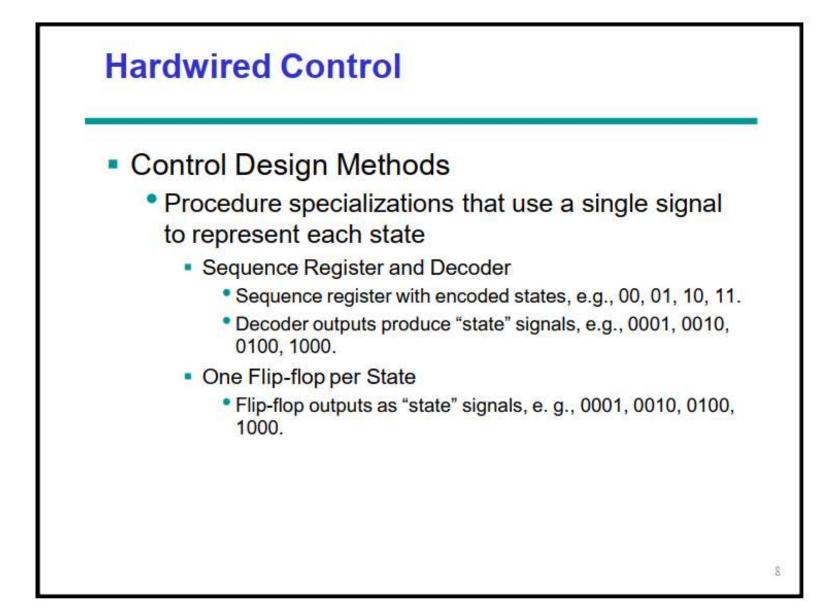
Block Diagram Module	Microope ration	Control Sign al N ame	Control Expression
Register A:	<i>A</i> ←0	Initialize	IDLE · G
_	$A \leftarrow A + B$	Load	MULO · Qo
	$C \parallel A \parallel Q \leftarrow \mathrm{sr} \ C \parallel A \parallel Q$	Shift_dec	MUL1
Register B:	$B \leftarrow IN$	Load_B	LOADB
Flip-Flop C:	<b>C</b> ← <b>0</b>	Clear_C	$IDLE \cdot G + MUL1$
	$C \leftarrow C_{\text{out}}$	Load	—
Register Q:	$\mathbf{Q} \leftarrow \mathbf{IN}$	Load_Q	LOADQ
	$C \parallel A \parallel Q \leftarrow \operatorname{sr} C \parallel A \parallel Q$	Shift_dec	1989) 1 <u>988</u> 1
Counter P:	$P \leftarrow n-1$	Initialize	-
	$P \leftarrow P - 1$	Shift_dec	—



- Signals are defined on a register basis
- LOADQ and LOADB: external signals controlled from the system using the multiplier and will not be considered a part of this design
- Many control signals are "reused" for different registers.
  - These 4 control signals are the "outputs" of the control unit: initialize, load, shift\_dec, clear\_c

# Multiplier Example - Sequencing Part of ASM





#### Multiplier Example: Sequencer and Decoder Design - Specification

- Initially, use sequential circuit design techniques
- First, define:
  - States: IDLE, MUL0, MUL1
  - Input Signals: G, Z, Q<sub>0</sub> (Q<sub>0</sub> affects outputs, not next state)
  - Output Signals: Initialize, LOAD, Shift\_Dec, Clear\_C
  - State Transition Diagram (Use Sequencing ASM)
  - Output Function: Use Control Signal Table
- Second, find
  - State Assignments
  - Use two state bits to encode the three states IDLE, MUL0, and MUL1.

State	M1	MO
IDLE	0	0
MUL0	0	1
MUL1	1	0
Unused	1	1

#### Multiplier Example: Sequencer and Decoder Design - Formulation

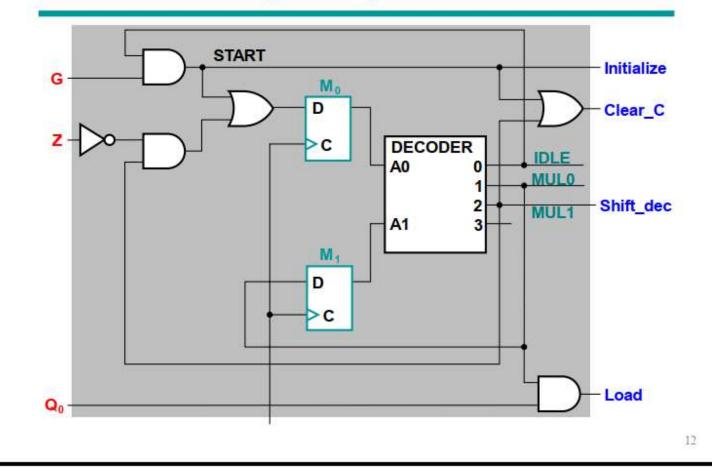
 Assuming that state variables M1 and M0 are decoded into states, the next state part of the state table is:

Current State	Input G Z	Next State M1 M0	Current State M1 M0	Input G Z	Next State M1 M0
IDLE	0 0	0 0	MUL1	0 0	0 1
IDLE	0 1	0 0	MUL1	0 1	0 0
IDLE	1 0	0 1	MUL1	1 0	0 1
IDLE	1 1	0 1	MUL1	1 1	0 0
MUL0	0 0	1 0	Unused	0 0	d d
MUL0	0 1	1 0	Unused	0 1	d d
MUL0	1 0	1 0	Unused	1 0	d d
MUL0	1 1	1 0	Unused	1 1	d d

#### Multiplier Example: Sequencer and Decoder Design – Equations Derivation/Optimization

```
Finding the equations for M1 and M0 using decoded states:
        M1 = MULO
        M0 = IDLE \cdot G + MUL1 \cdot \overline{7}
The output equations using the decoded states:
     Initialize = IDLE \cdot G
     Load = MUL0 \cdot Q_0
     Clear C = IDLE · G + MUL1
     Shift dec = MUL1
Doing multiple level optimization, extract IDLE · G:
      START = IDLE \cdot G
     M1 = MUL0
      M0 = START + MUL1 \cdot \overline{Z}
     Initialize = START
     Load = MUL0 \cdot Q_0
     Clear C = START + MUL1
     Shift dec = MUL1
 The resulting circuit using flip-flops, a decoder, and the above
  equations is given on the next slide.
```

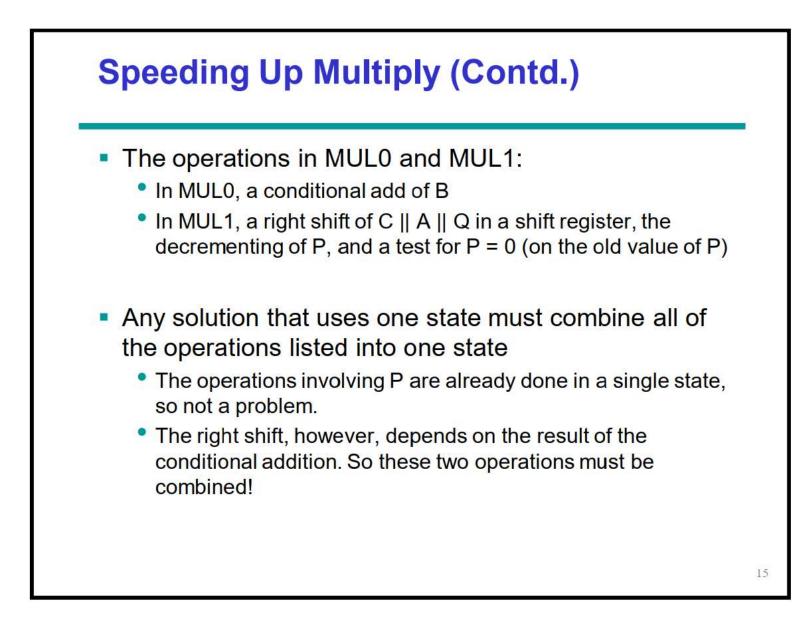
#### Multiplier Example: Sequencer and Decoder Design - Implementation

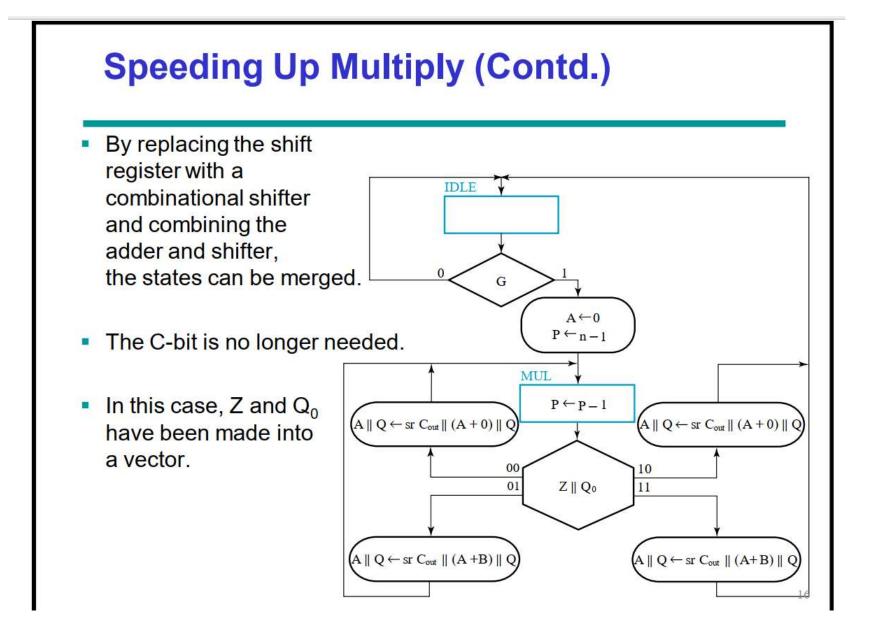


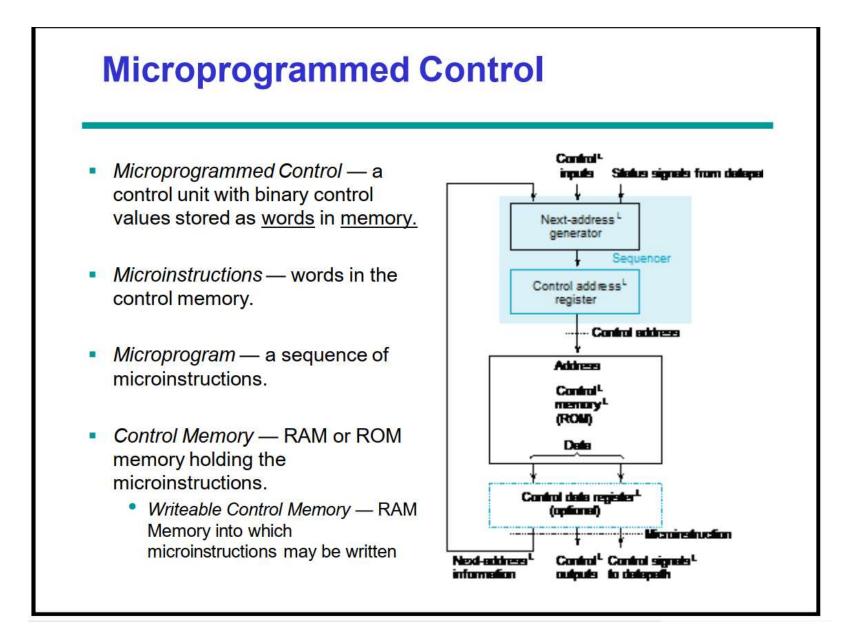
Binary multiplier with n=4	No. AL MARINESS IN THE REPORTATION
library ieee;	datapath_func : process (CLK)
use ieee.std_logic_unsigned.all;	variable CA: std_logic_vector (4 downto 0);
entity binary multiplier is	begin
port(CLK, RESET, G, LOADB, LOADQ: in std_logic;	if (CLK'event and CLK='1') then
MULT_IN : in std_logic_vector (3 downto 0);	if LOADB='1' then
MULT_OUT : out std_logic_vector (7 downto 0));	$B \le MULT IN:$
end bianry_multiplier;	The state of the s
	end if;
architecture behavior_4 of binary_multiplier is	if $LOADQ = '1'$ then
type state_type is (IDLE, MUL0, MUL1); variable P:=3;	$Q \leq MULT_IN;$
signal state, next_state : state_type;	end if;
signal A, B, Q:std_logic_vector(3 downto 0);	case state is
signal C, Z:std_logic;	when IDLE =>
begin y g y	if G = '1' then
$Z \le P(1) \text{ NOR } P(0);$	C <= '0';
$MULT_OUT \le A \& Q;$	A <= "0000";
(CIV PECET)	P <= "11":
state_register : process (CLK, RESET) begin	end if;
if (RESET = '1') then	when MUL0 =>
state <= IDLE;	if $Q(0) = 1$ then
elsif (CLK'event and CLK='1') then	CA := ('0' & A) + ('0' & B);
<pre>state &lt;= next_state;</pre>	
endif;	else
end process;	CA := C & A;
	end if;
next_state_func : process (G, Z, state)	C <= CA(4);
begin case state is	A <= CA(3 downto 0);
when IDLE =>	when MUL1 =>
if G='1' then next_state <= MUL0;	C <= '0';
else next_state <= IDLE;	$A \leq C \& A(3 \text{ downto } 1);$
end if;	$Q \le A(0) \& Q(3 \text{ downto } 1);$
when MUL0 =>	P <= P - "01":
next_state <= MUL1;	end case;
when MUL1 =>	end if;
if Z='1' then next_state <= IDLE;	
else next_state <= MUL0; end if;	end process;
end case;	
end process;	end behavior_4;
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### **Speeding Up the Multiplier**

- In processing each bit of the multiplier, the circuit visits states MUL0 and MUL1 in sequence.
- By redesigning the multiplier, is it possible to visit only a single state per bit processed?







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1

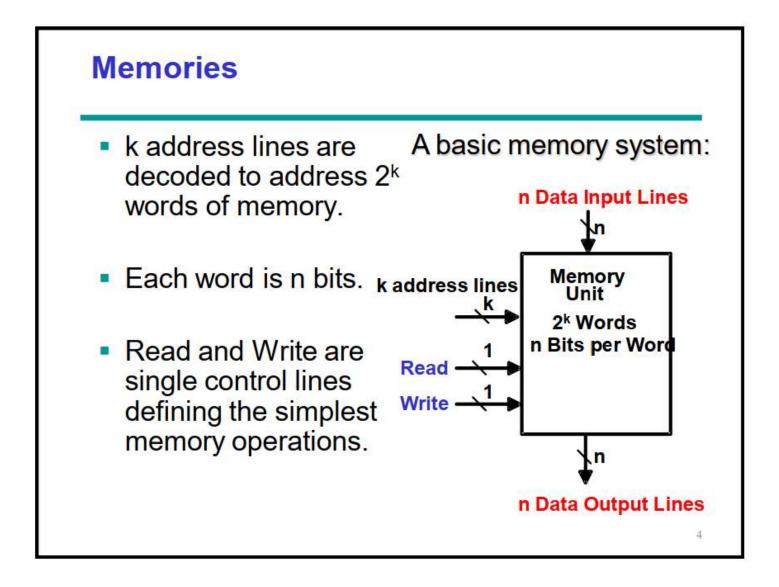
# Digital System Design II Memories Overview

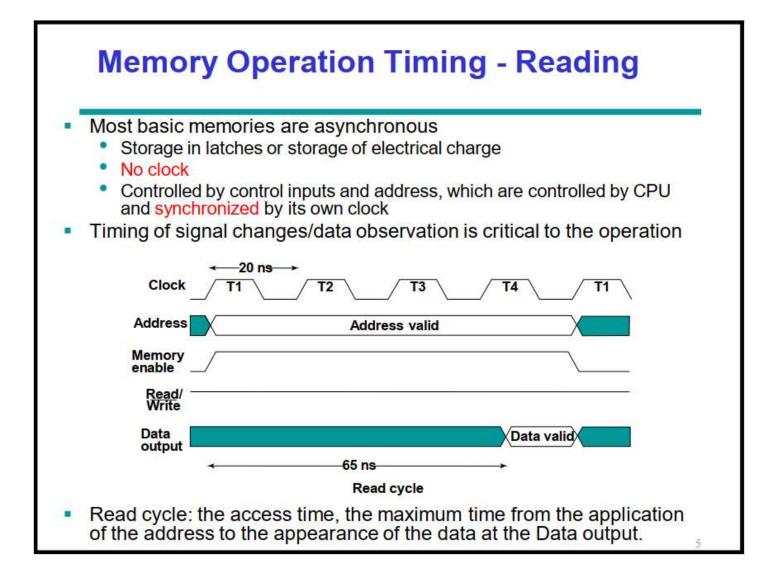
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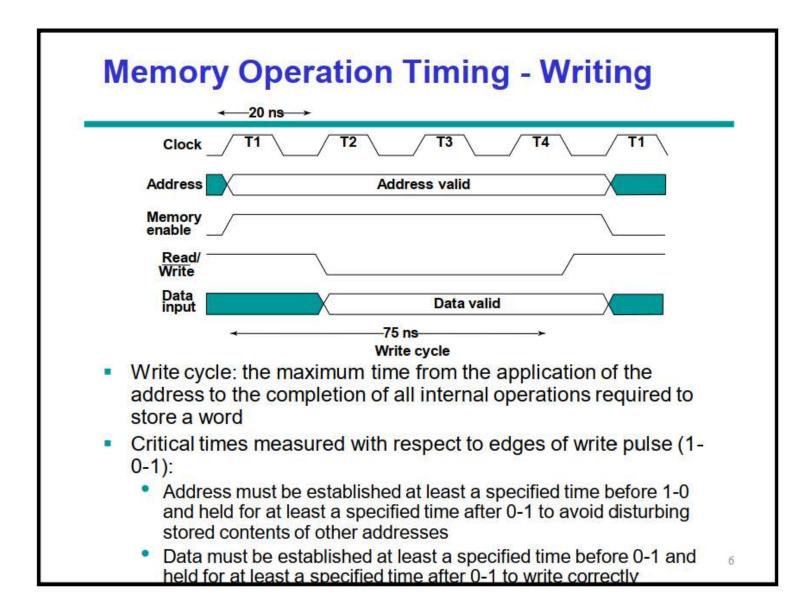
#### **Memories**

F	Read-Write Memory	6	Read-Only Memory
Volati	Volatile Memory		
Random Access	Sequential Access	EPROM EEPROM FLASH	Mask-Programmed ROM (PROM) (nonvolatile)
DRAM SRAM	FIFO LIFO Shift Register CAM		

- Volatile: need electrical power
- · Nonvolatile: magnetic disk, retains its stored information after the removal of power
- · Random access: memory locations can be read or written in a random order
- EPROM: erasable programmable read-only memory
- EEPROM: electrically erasable programmable read-only memory
- FLASH: memory stick, USB disk
- Access pattern: sequential access: (video memory streaming) first-in-first-out (buffer), last-infirst-out (stack), shift register, content-addressable memory





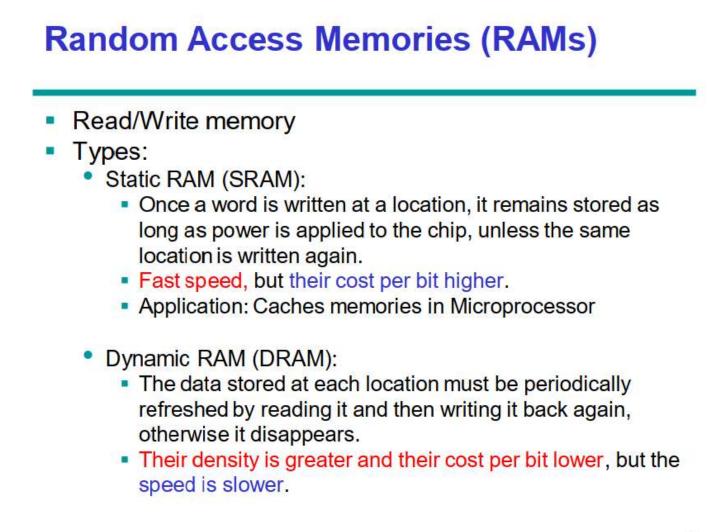


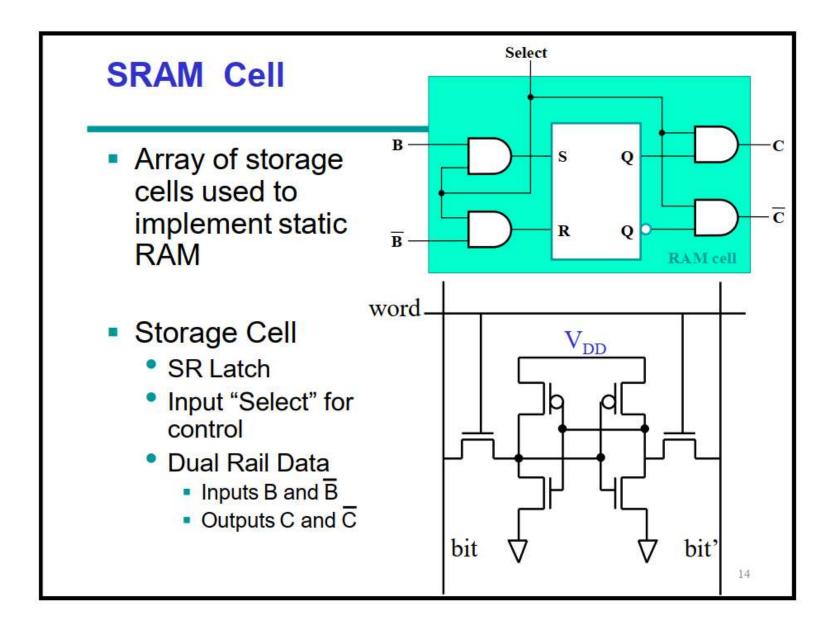
#### VHDL code for ROM

library IEEE; use IEEE.std\_logic\_1164.all;

ENTITY rom8x4 IS PORT ( addr: in std\_logic\_vector(2 downto 0); q: out std\_logic\_vector(3 downto 0)); END rom8x4; ARCHITECTURE behav OF rom8x4 IS BEGIN

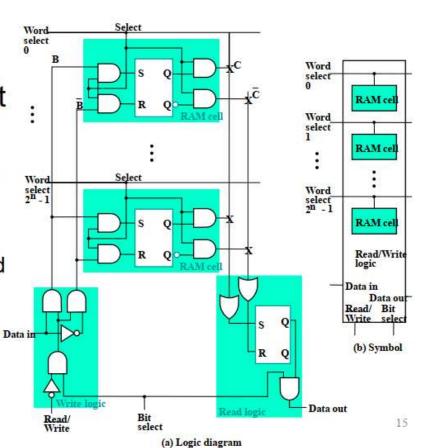
#### PROCESS(addr) BEGIN CASE addr IS when "000" => q <= "0001"; when "001" => q <= "0000"; when "010" => q <= "0111"; when "011" => q <= "1101"; when "100" => q <= "1000"; when "101" => q <= "1000"; when "111" => q <= "1010"; when "111" => q <= "1011"; when others => NULL; END case; END process; END behav;





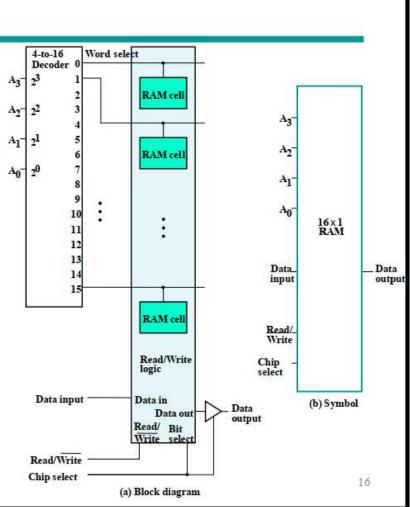
#### **SRAM Bit Slice**

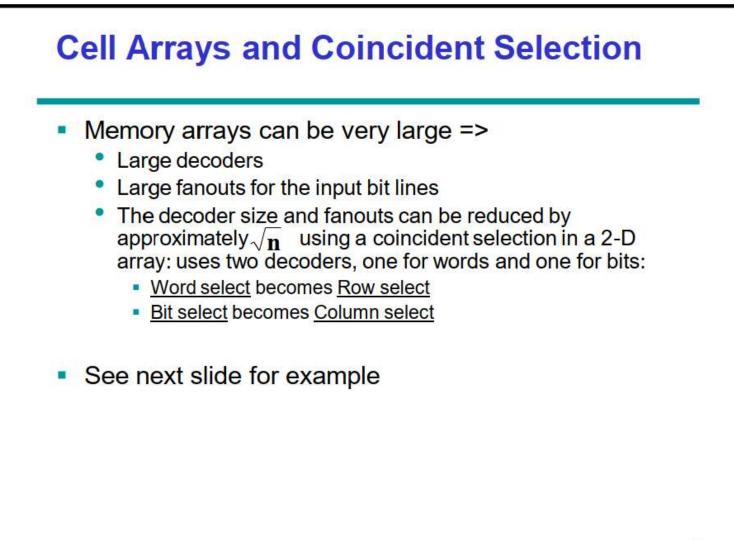
- Represents all circuitry that is required for 2<sup>n</sup> 1-bit words
  - Multiple RAM cells
  - Control Lines:
    - Word select i
      - one for each word
    - Read/Write
    - Bit Select
  - Data Lines:
    - Data in
      - Data out



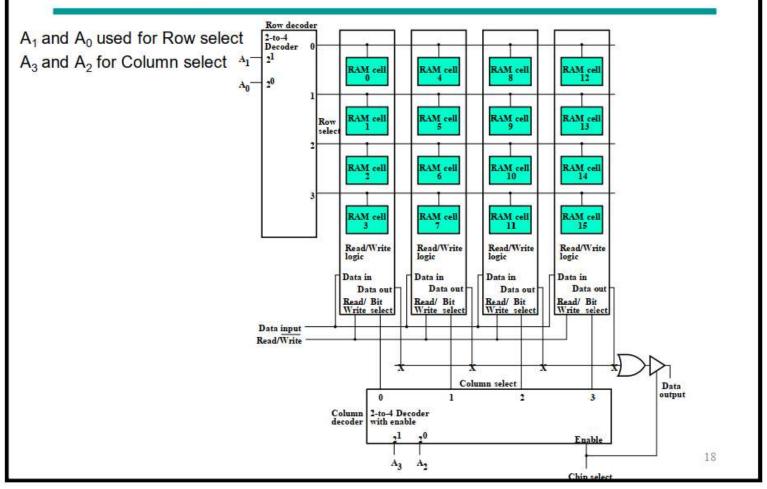
#### 2<sup>n</sup>-Word by 1-Bit RAM IC

- To build a RAM IC from a RAM slice:
  - <u>Decoder</u> decodes the n address lines to 2<sup>n</sup> word select lines
  - A <u>3-state buffer</u> on the data output permits RAM ICs to be combined into a RAM with c × 2<sup>n</sup> words



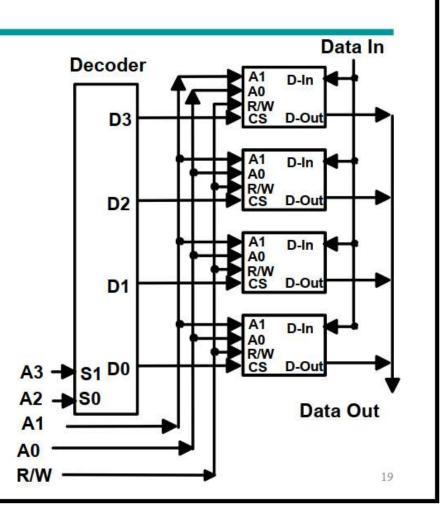


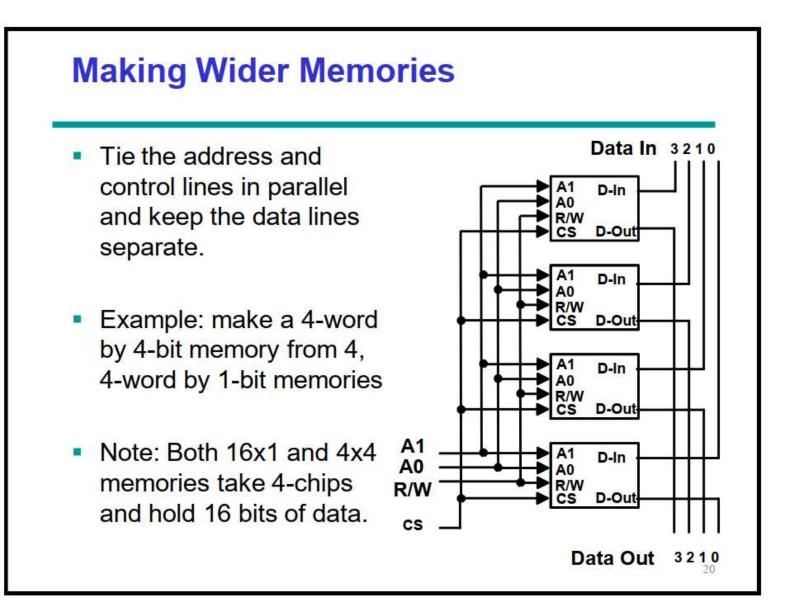
# Cell Arrays and Coincident Selection (Contd.)

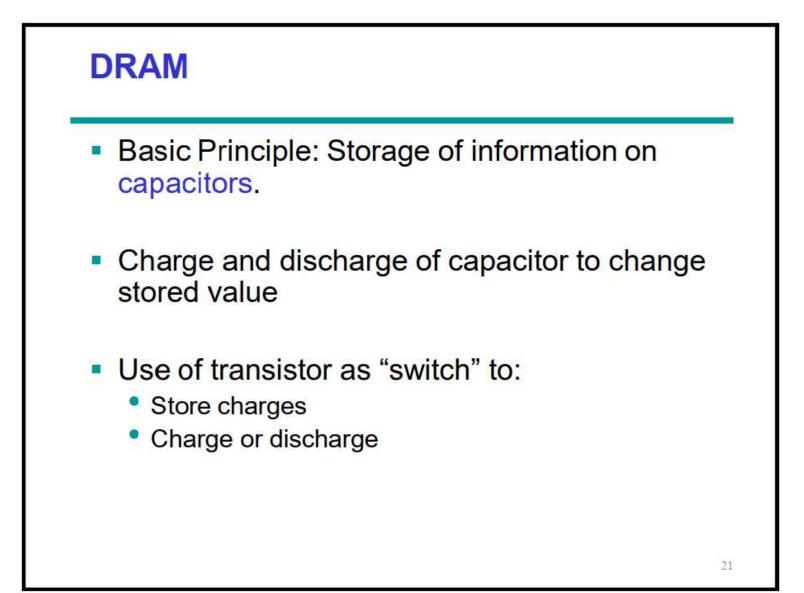


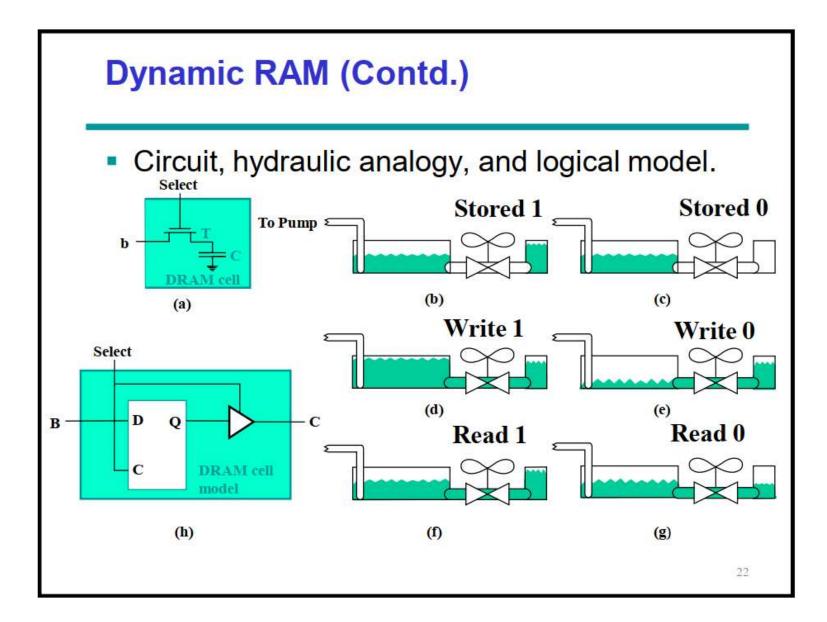
#### **Making Larger Memories**

- We can make larger memories from smaller ones by using the decoded higher order address bits to control CS (chip select) lines, tying all address, data, and R/W lines in parallel.
- A 16-Word by1-Bit memory constructed using 4-Word by 1-Bit memory.



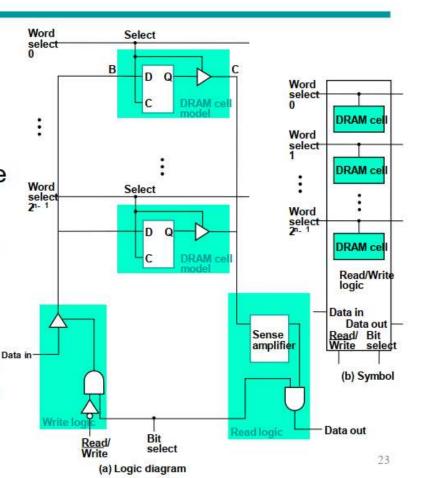






#### **Dynamic RAM - Bit Slice**

- C driven by 3-state drivers
- Sense amplifier is used to change the small voltage change on C into H or L
- In the electronics, B, C, and the sense amplifier output are connected to make destructive read into Data innon-destructive read



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### Digital System Design II Microprogramming

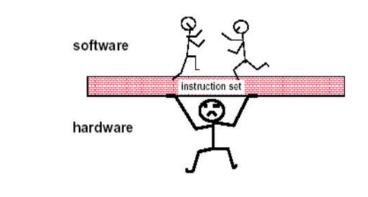
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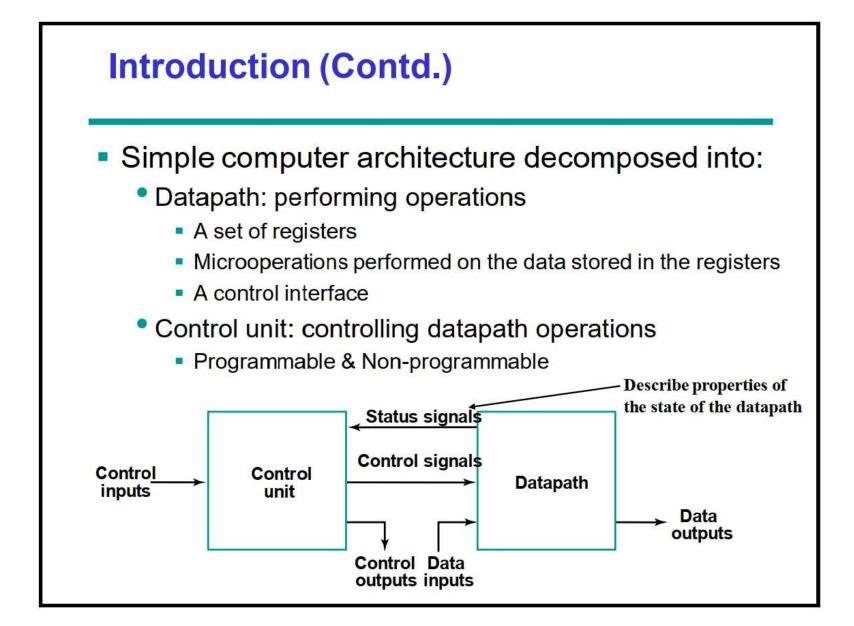
#### **Microprogramming Overview**

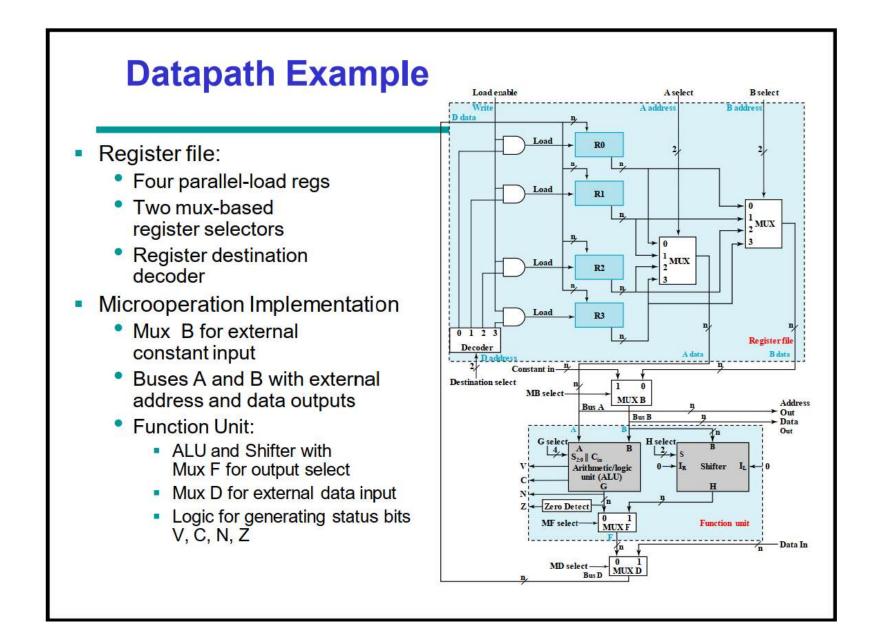
- Part 1 Datapaths
  - Introduction
  - Datapath Example
    - Arithmetic Logic Unit (ALU)
    - Shifter
  - Datapath Representation and Control Word
- Part 2 A Simple Computer
  - Instruction Set Architecture (ISA)
  - Single-Cycle Hardwired Control
- Part 3 Multiple Cycle Hardwired Control
  - Single Cycle Computer Issues
  - Sequential Control Design

#### Introduction

- Computer Specification
  - Instruction Set Architecture (ISA) the specification of a computer's appearance to a programmer at its lowest level
  - Computer Architecture a high-level description of the hardware implementing the computer derived from the ISA
  - The architecture usually includes additional specifications such as speed, cost, and reliability.



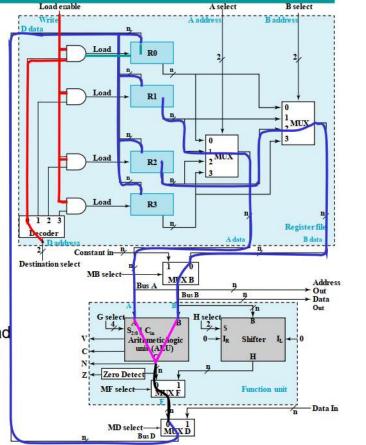




## Datapath Example: Performing a Microoperation

Microoperation:  $R0 \leftarrow R1 + R2$ 

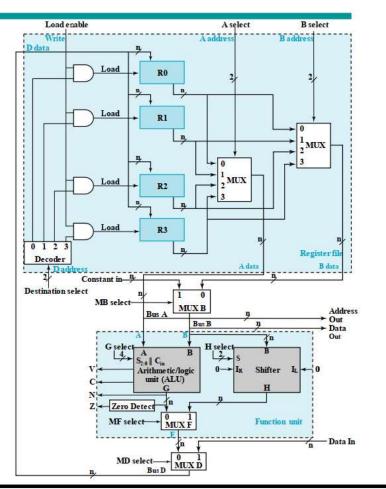
- Apply 01 to A select to place contents of R1 onto Bus A
- Apply 10 to B select to place contents of R2 onto B data and apply 0 to MB select to place B data on Bus B
- Apply 0010 to G select to perform addition G = Bus A + Bus B
- Apply 0 to MF select and 0 to MD select to place the value of G onto BUS D
- Apply 00 to Destination select to enable the Load input to R0
- Apply 1 to Load Enable to force the Load input to R0 to 1 so that R0 is loaded on the clock pulse (not shown)
- The overall microoperation requires 1 clock cycle

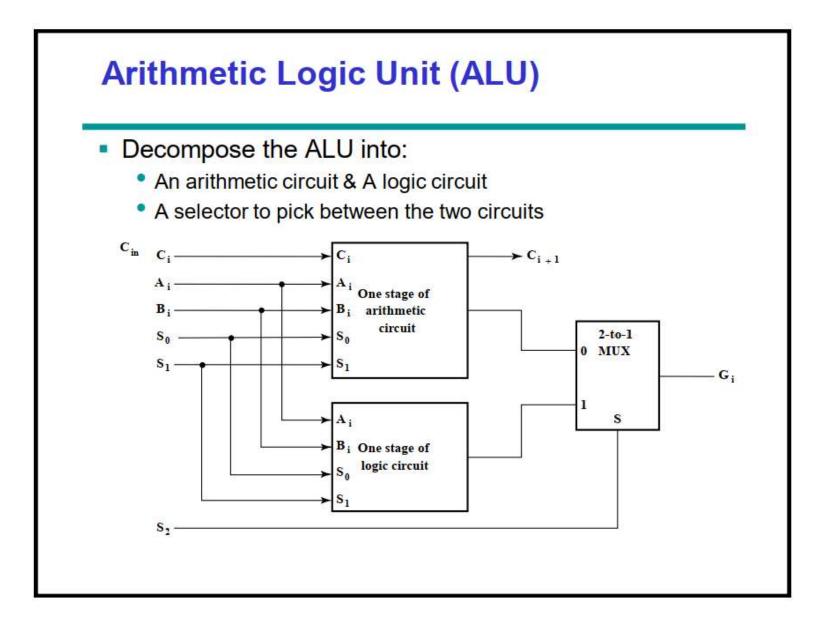


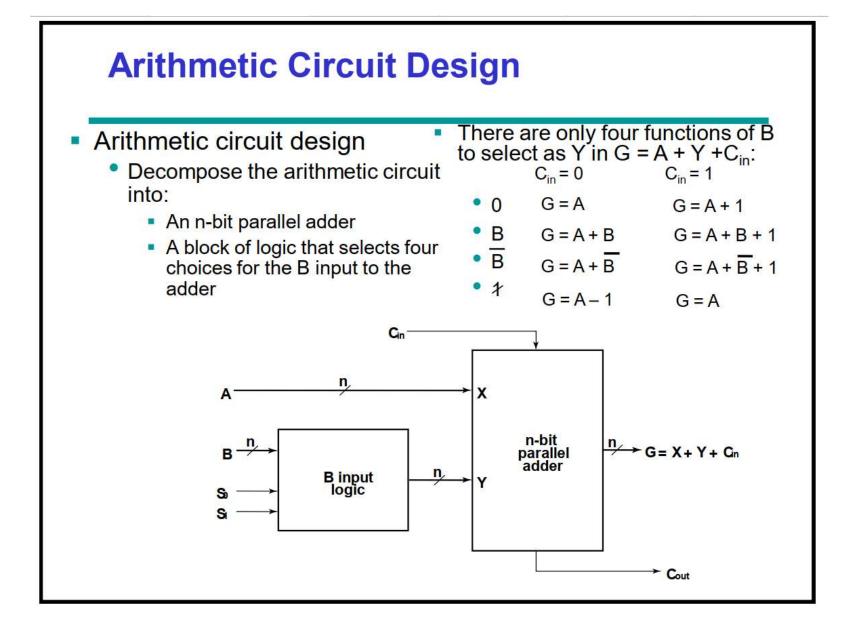
#### Datapath Example: Key Control Actions for Microoperation Alternatives

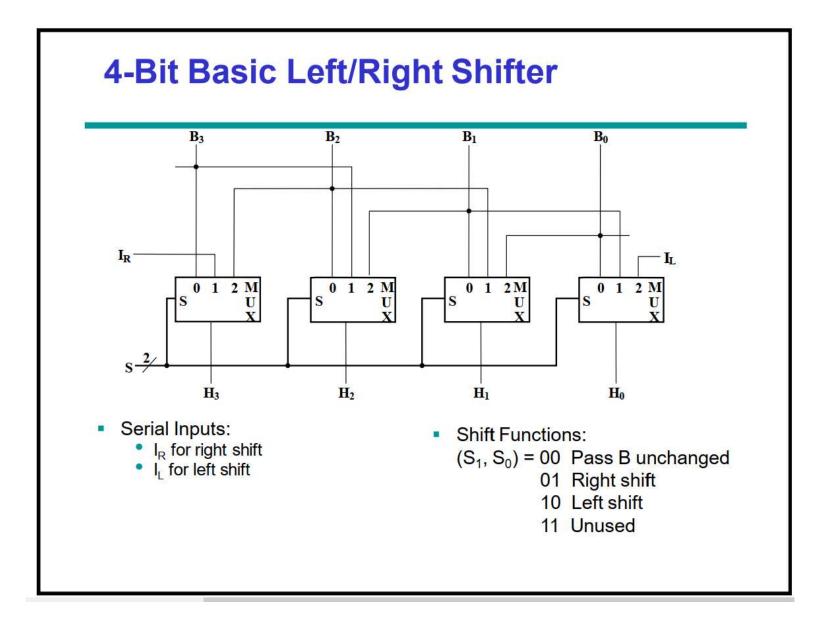
Various microoperations:

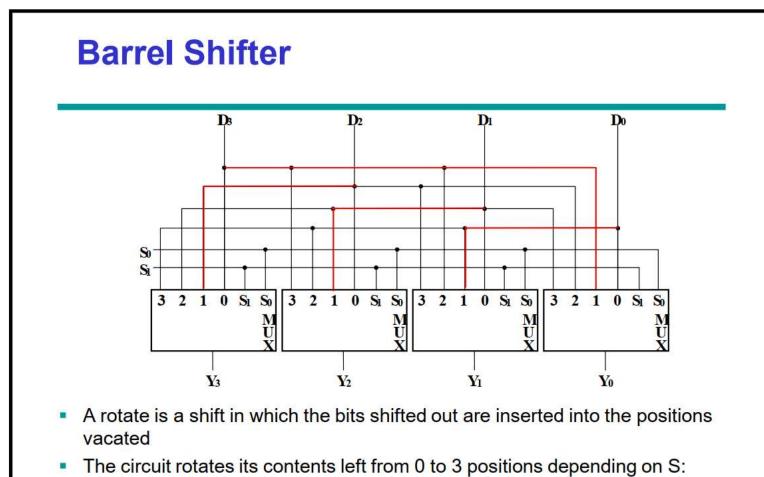
- Perform a shift microoperation: apply 1 to MF select
- Use a constant in a micro-operation using Bus B: apply 1 to MB select
- Provide an address and data for a memory or output write microoperation – apply 0 to Load enable to prevent register loading
- Provide an address and obtain data for a memory or output read microoperation – apply 1 to MD select
- For some of the above, other control signals become don't cares











- S = 00 position unchanged
- S = 10 rotate left by 2 positions
- S = 01 rotate left by 1 positions
- S = 11 rotate left by 3 positions

