

③ Sparking Voltage - Paschen's Law :-

According to Townsend's theory the breakdown criterion for gases is given as

$$\gamma [\exp(\alpha d) - 1] = 1$$

Where: the coefficient α and γ are functions of p & E/p

important relationship between breakdown voltage of the gas and p and d . where d is the gap length. While deriving the relationship said above the made some approximations, i.e.

$$\frac{\alpha}{p} = f_1(E/p)$$

$$\text{and } \gamma = f_2(E/p)$$

We know that electric field in the gap between electrodes supplied with V volts is

$$E = V/d$$

Substituting E in α/p & γ expressions and then rewriting Townsend's criterion for Breakdown in gases we get,

$$\frac{\gamma}{p} = f_1(E/p) = f_2(V/pd) \Rightarrow \alpha = p \cdot f_1(V/pd)$$

$$\text{and } \gamma = f_2(E/p) = f_2(V/pd)$$

$$\gamma [\exp(\alpha d) - 1] = 1$$

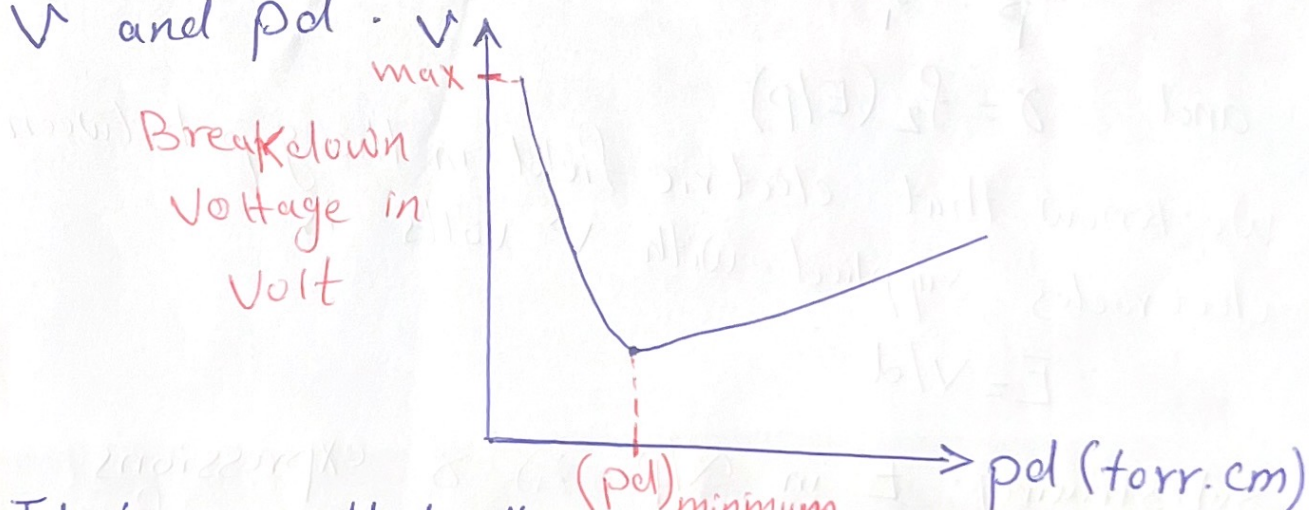
$$\Rightarrow f_2(V/pd) \left\{ \left[\exp(pd \cdot f_1(V/pd)) - 1 \right] \right\} = 1$$

This equation shows a relationship between V & pd and implies that the Breakdown Voltage varies as the product p and d i.e. pd varies.

$$V = f(pd)$$

This equation is known as Paschen's Law

The graph below shows the relationship between V and pd .



It is seen that the relationship between V and pd is not linear and has a minimum value for any gas.

This means that a breakdown voltage of a uniform field gap is unique function of p and pd .

For a particular gas and particular material used in making electrodes.

The minimum point in the graph is due to transition from Townsend's mechanism to streamer mechanism.

In order to account for the effect of temperature the Paschen's law is generally stated as

$$V = f(Nd),$$

Where: N is the density of gas molecules.

This is necessary the pressure because the gas changes with temperature according to the gas-law

$PV = NRT$, Where V is the volume of the gas, T is the temperature of the gas and R is a constant

Based on experimental results, the breakdown potential of air is expressed as a power function in $p \cdot d$ as

$$V = 24.22 \left[\frac{293 p d}{760 T} \right] + 6.08 \left[\frac{293 p d}{760 T} \right]^{1/2}$$

In above expression if we put $p = 760$ torr and $T = 293$ K we get,

$$E = \frac{V}{d} = 24.22 + \left[\frac{6.08}{\sqrt{d}} \right] \text{ kV/cm}$$

and this equation gives limiting values for E for long gap as,

$$E = V/d = 24 \text{ kV/cm}$$

and $E = 30 \text{ kV/cm}$ for $\left(\frac{293 \text{ Pd}}{760 \text{ T}}\right) = 1,$

Which means a pressure of 760 torr at 20°C with 1 cm gap. This is usually get breakdown strength of air at room temperature and at 1 atmospheric pressure.

Partial Breakdown and Corona:-

ظاهرة تحدث في خطوط النقل العالي تسبب ظاهرة كورونا
(ظاهرة الهالة التي تحيط بخطوط النقل الكهربائي) فوق 30KV
تعتبر ظاهرة تفريغ للشحنات

Corona: When an alternating potential difference is applied across two conductors whose spacing is large as compared to their diameters, there is no apparent change in the condition of atmospheric air surrounding the wires if the applied voltage is low. However, when the applied voltage exceeds a certain value, called **Critical disruptive voltage**, the conductors are surrounded by a faint violet glow called **Corona**.

تصاب هذه الظاهرة عند أشكال من الحالات :-

The phenomenon of Corona is accompanied by:
1. Hissing Sound, 2. production of OZONE, 3. Power loss and 4. Radio interference. (noise)

عند تسليط تيار متناوب على موصلين عندما يكون البعد بينهما أكبر من القطر المركزي فإحدى الحالة لا تظهر أي شحنة في الهواء الجوي حول الأسلاك

← تعتبر ظاهرة Corona على تآكل الأسلاك سببها العولسة العالية الموجودة في خطوط النقل باللون البنفسجي ولكن عندما ترتفع قيمة العولسة للأسلاك الكاملة بواسطة خطوط النقل تظهر هذه الظاهرة حولها وتكون باللون البنفسجي.

The higher voltage is raised, the larger and higher of luminous envelope becomes, and greater are the sound, power loss and radio noise. If the applied voltage is increased to breakdown value with flash-over will occur between the conductors due to the breakdown of air insulation.

The phenomenon of Violet glow, hissing noise and production of Ozone gas in an Overhead transmission line is known as Corona.

If the conductors are polished and smooth, the Corona glow will be uniform throughout the length of the conductors, otherwise the rough points will appear brighter. With d.c voltage, there is difference in the appearance of the two wires. The positive wire has uniform glow about it, while the negative conductor has Spotty glow. جيات فتوهجة.

Factors Effecting on Corona :- العوامل المؤثرة

The phenomenon of Corona is affected by the physical state of the atmosphere as well as by the conditions of the line. The following are the factors upon which Corona depends:

1. Atmospheric
2. Conductor size
3. Spacing between conductors
4. line voltage

MATHEMATICAL-TERMS:-

The phenomenon of Corona is important in the design of an overhead transmission line. Therefore, it is profitable to consider the following terms much used in the analysis of Corona effects:-

1. **Critical disruptive Voltage:-** It is the minimum phase neutral voltage at which Corona occurs. Consider two conductors of radii r cm and spaced d cm apart. If V is the phase-neutral potential, then potential gradient at the conductor surface is given by:-

$$g = \frac{V}{r \log_e \frac{d}{r}} \text{ Volts/cm}$$

V: critical disruptive voltage

In order that Corona is formed, the value of g must be made equal to the breakdown strength of air. The breakdown strength of air at 76 cm pressure and temperature of 25°C is 30 kV/cm (max) or $21.2 \text{ kV/cm (r.m.s)}$ and is denoted by g_0 . If V_c is the phase-neutral potential required under these conditions,

then

$$g_0 = \frac{V_c}{r \log_e \frac{d}{r}}$$

Where: g_0 = breakdown strength of air at 76 cm of mercury at 25°C

= 30 kV/cm (max) or $21.2 \text{ kV/cm (r.m.s)}$

$$\therefore \left[\text{Critical disruptive voltage, } V_c = g_0 r \log_e \frac{d}{r} \right]$$

The above expression for disruptive voltage is under standard conditions i.e., at 76 cm of Hg and 25°C . However, if these conditions vary, the air density also changes, thus altering the value of g_0 .

The value of g_0 is directly proportional to air density. Thus the breakdown strength of air at a barometric pressure of b cm of mercury and temperature of $t^{\circ}\text{C}$ becomes $\delta = \text{sigma}$

Where $\delta = \text{air density factor} = \frac{3.926}{273+t}$

Under standard conditions, the value of $\delta = 1$.

Critical disruptive voltage, $\left[V_c = g_0 \delta r \log_e \frac{d}{r} \right]$ At standard condition

Correction must also be made for the surface condition of the conductor. This is accounted for by multiplying the above expression by irregularity factor m_0 . (تصحیح هذا المثل في انتظام السطح: m_0 او عدم انتظامه)

$\therefore$ Critical disruptive voltage, $V_c = m_0 g_0 \delta r \log_e \frac{d}{r}$ KV/phase

Where $m_0 = 1$ for polished conductors.
 $= 0.98$ to 0.92 for dirty conductors.
 $= 0.87$ to 0.8 for standard conductors.

2. Visual Critical Voltage:- It is the minimum phase-neutral voltage at which corona glow appears all along the line conductors. It has been seen that in case of parallel conductors, it has the corona glow does not begin at disruptive voltage V_c but at a higher voltage V_r , called Visual Critical Voltage. The phase-neutral effective value of visual voltage is given by the following empirical formula:-

$$V_r = m_v g_0 \delta r \left[1 + \frac{0.3}{\sqrt{\delta r}} \right] \log_e \frac{d}{r} \text{ KV/phase}$$

Where: m_v is another irregularity factor having a value of 0.1 for polished conductors and 0.72 to 0.82 for rough conductors.

3. Power loss due Corona:- Formation of Corona is always accompanied by energy loss which is dissipated in the form of light, heat, sound and chemical action. When disruptive voltage is exceeded the power loss due to Corona is given by

$$P = 242.2 \left[\frac{f + 25}{8} \right] \sqrt{\frac{r}{d}} (V - V_c)^2 \times 10^{-5} \text{ KW/km/phase}$$

Where: f = supply frequency in HZ

V = phase-voltage neutral (r.m.s)

V_c = disruptive voltage (r.m.s) per phase

تسبب ظاهرة Corona ضائري في العولسية المتولدة في الأسلاك
النقل العاليه ولكن نقل على تحليل هذه الظاهرة تطلب عدة نظريات
هنا :-

METHODS OF REDUCING CORONA EFFECT:-

It has been seen that intense corona effects are observed at working voltage of 33kV or above. Therefore, careful design should be made to avoid corona on the sub-stations or busbars rated for 33kV and higher voltages otherwise highly ionized air may cause flash-over in the insulators or between the phases, causing considerable damage to the equipment. The corona effect can be reduced by the following methods:-

يسبب انحراف قوي في المعدات

1. By increasing conductor size: By increasing conductor size, the voltage at which corona occurs is raised and hence corona effects are considerably reduced. This is one of the reasons that ACSR conductors which have a larger cross-sectional area are used in transmission line.

نوع الكابل المستعمل يكون الألومنيوم في وسط
داخلياً بالستيل

2. By increasing conductor spacing:-
By increasing conductor spacing between conductors, the voltage at which corona occurs is raised and hence corona effects can be eliminated. However, spacing cannot be increased too much otherwise the cost of supporting structure (e.g, bigger cross arms and supports) may increase to a considerable extent.

Example:- 8.13

A 3-phase line has conductors 2cm in diameter spaced equilaterally 1m apart. If the dielectric strength of air is 30kV(max) per cm, find the disruptive critical voltage for the line. Take air density factor $\delta = 0.952$ and irregularity factor $m_0 = 0.9$?

Solution.

Conductor radius, $r = 2/2 = 1 \text{ cm}$

Conductor spacing, $d = 1 \text{ m} = 100 \text{ cm}$

Dielectric strength of air, $g_0 = 30 \text{ kV/cm (max.)}$
 $= 21.2 \text{ kV (r.m.s) per cm}$

Disruptive critical voltage, $V_c = m_0 g_0 \delta r \log_e (d/r)$

kV/phase [(r.m.s) Value]

$$\therefore V_c = 0.9 \times 21.2 \times 0.952 \times 1 \times \log_e 100/1 = 83.64 \text{ kV/phase}$$

$$\therefore \text{line voltage (r.m.s)} = \sqrt{3} \times 83.64 = 144.8 \text{ kV}$$

Example: 8.14 A 132 kV line with 1.956 cm dia. conductors is built so that corona takes place if the line voltage exceeds 210 kV (r.m.s). If the value of potential gradient at which ionization occurs can be taken as 30 kV per cm. find the spacing between the conductors.

Solution. Assume the line is 3-phase

Conductor radius, $r = 1.956/2 = 0.978 \text{ cm}$

Dielectric strength of air, $g_0 = 30/\sqrt{2} = 21.2 \text{ kV (r.m.s) per cm}$

Disruptive critical voltage, $V_c = 210/\sqrt{3} = 121.25 \text{ V}$

Assume smooth conductors (i.e. irregularity factor $m_0 = 1$) and standard pressure and temperature for which air density factor $\delta = 1$. Let $d \text{ cm}$ be the spacing between the conductors. $\therefore$ Disruptive voltage (r.m.s) per phase is

$$V_c = m_0 g_0 \delta r \log_e (d/r) \text{ kV}$$

$$= 1 \times 21.2 \times 1 \times 0.978 \times \log_e (d/r)$$

$$121.25 = 20.733 \log_e (d/r)$$

$$\text{or } \log_e \frac{d}{r} = \frac{121.25}{20.733} = 5.848$$

$$\text{or } 2.3 \log_{10} d/r = 5.848$$

$$\log_{10} d/r = 5.848 / 2.3 = 2.5426$$

$$d/r = \text{Antilog } 2.5426$$

$$d/r = 348.8$$

∴ Conductor spacing

$$d = 348.8 \times r = 348.8 \times 0.978 = 341 \text{ cm}$$

Example: 8.15. A 3-phase, 220kV, 50Hz transmission line consists of 1.5 cm radius conductor spaced 2 meters apart in equilateral triangular formation. If the temperature is 40°C and atmospheric pressure is 76 cm. Calculate the Corona loss per km of the line. Take $m_0 = 0.85$?

Solution.

As seen from art. 8.12, the corona loss is given by:

$$P = \frac{242.2}{\delta} (\delta + 25) \sqrt{\frac{r}{d}} (V - V_c)^2 \times 10^{-5} \text{ kw/km/phase}$$

$$\text{Now, } \delta = \frac{3.926}{273 + t} = \frac{3.92 \times 76}{273 + 40} = 0.952$$

Assuming, $g_0 = 21.2 \text{ kv/cm (r.m.s)}$

$\therefore$ Critical disruptive voltage per phase is

$$V_c = m_0 g_0 \delta r \log_e \frac{d}{r} \text{ kv}$$

$$= 0.85 \times 21.2 \times 0.952 \times 1.5 \times \log_e \frac{200}{1.5} = 125.9 \text{ kv}$$

Supply voltage per phase,

$$V = 220/\sqrt{3} = 127 \text{ kv}$$

Substituting the above values, we have Corona loss as:

$$P = \frac{242}{0.952} (50 + 25) \times \sqrt{\frac{1.5}{200}} \times (127 - 125.9)^2 \times 10^{-5} \text{ kw/ph/km}$$

$$= 0.01999 \text{ kw/km/phase}$$

$\therefore$ Total Corona loss per km for three phases.

$$= 3 \times 0.01999 \text{ kw} = 0.05998 \text{ kw}$$

Homeworks

① Estimate the corona loss for three-phase, 110 kV, 50 Hz 150 km long transmission line consisting of three conductors each of 10 mm diameter and spaced 2.5 m apart in an equilateral triangle formation. The temperature of air is 30°C and the atmospheric pressure is 750 mm of mercury. Take irregularity factor as 0.85. Ionization of air may be assumed to take place at a maximum voltage gradient of 30 kV/cm.

② Taking the dielectric strength of air to be 30 kV/cm, calculate the disruptive critical voltage for a 3-phase line with conductors of 1 cm radius and spaced symmetrically 4 m apart.

③ A 3-phase, 220 kV, 50 Hz transmission line consists of 1.2 cm radius conductors spaced 2 m at the corners of an equilateral triangle. Calculate the corona loss per km of the line. The condition of the wire is smoothly weathered and the weather is fair with temperature of 20°C and barometric pressure of 72.2 cm of Hg.